Hybrid-maize—a maize simulation model that combines two crop modeling approaches

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Abstract

A new maize (Zea mays L.) simulation model, Hybrid-Maize, was developed by combining the strengths of two modeling approaches: the growth and development functions in maize-specific models represented by CERES-Maize, and the mechanistic formulation of photosynthesis and respiration in generic crop models such as INTERCOM and WOFOST. It features temperature-driven maize phenological development, vertical canopy integration of photosynthesis, organ-specific growth respiration, and temperature-sensitive maintenance respiration. The inclusion of gross assimilation, growth respiration and maintenance respiration makes the Hybrid-Maize model potentially more responsive to changes in environmental conditions than models such as CERES-Maize. Hybrid-Maize also requires fewer genotype-specific parameters without sacrificing prediction accuracy. A linear relationship between growing degree-days (GDD) from emergence to silking and GDD from emergence to physiological maturity was used for prediction of day of silking when the former is not available. The total GDD is readily available for most commercial maize hybrids. Preliminary field evaluations at two locations under high-yielding growth conditions indicated close agreement between simulated and measured values for leaf area, dry matter accumulation, final grain and stover yields, and harvest index (HI). Key areas for further model improvement include LAI prediction at high plant density, and biomass partitioning, carbohydrate translocation, and maintenance respiration in response to above-average temperature, especially during reproductive growth. The model has not been evaluated under conditions of water and/or nutrient stress, and efforts are currently in progress to develop and validate water and nitrogen balance components for the Hybrid-Maize model.

Keywords: Crop models; Crop simulation; Yield potential; Zea mays L.

1. Introduction

Crop simulation models are mathematical representations of plant growth processes as influenced by interactions among genotype, environment, and crop management. They have become an indispensable tool for supporting scientific research, crop management, and policy analysis (Fischer et al., 2000; Hammer et al., 2002; Hansen, 2002). Simulation models serve different purposes, and the intended purpose influences the level of detail needed for mechanistic description of key processes, sensitivity to environment and management, data requirements, and model outputs. All cereal crop models must simulate plant growth and development, biomass partitioning among organs (leaves, stem, root, and reproductive structures),
and yield formation. The accuracy of simulating the outcome of these processes across a wide range of environments depends on basic understanding of the key ecophysiological processes and incorporating this knowledge in the mathematical formulations that constitute the model. For example, accurate prediction of carbon (C) sequestration scenarios in a given cropping system requires robust simulation of grain and stover yields, and the amount of assimilate partitioned belowground to root biomass and exudation (Cassman et al., 2003).

Different approaches have been used for simulating maize (Zea mays L.) development and growth. Generic crop models describe the processes of assimilation, respiration, development and growth without regard to crop species, and are then fine-tuned to simulate the phenological and physiological traits of specific crops such as maize, rice, or potatoes. Examples of generic crop models include SUCROS, WOFOST and INTERCOM (van Ittersum et al., 2003), STICS (Brisson et al., 2003), and CropSyst (Stöckle et al., 2003). In contrast to generic models, other crop models have been developed to simulate growth and development of a specific crop species. The CERES-Maize model and its implementation in DSSAT (Jones and Kiniry, 1986; Jones et al., 2003), and the Muchow–Sinclair–Bennett (MSB) model (Muchow et al., 1990) are examples of maize-specific models.

Maize-specific simulation models differ considerably from generic models in both theoretical framework and treatment of key processes that drive growth and development. For example, INTERCOM (Kropff and van Laar, 1993; Lindquist, 2001) distinguishes only two phases—the vegetative phase from emergence to anthesis and the reproductive phase from anthesis to maturity—and requires input of growing degree-days (GDD) for the duration of both phases. In contrast, CERES-Maize distinguishes five development stages—emergence to end of juvenile stage, the end of juvenile stage to tassel initiation, tassel initiation to silking, silking to effective grainfilling, and effective grainfilling to physiological maturity—and requires cultivar-specific input parameters for the GDD interval from emergence to the end of the juvenile phase, photoperiod sensitivity, and the duration of silking to maturity in GDD. Two additional cultivar-specific input parameters are required for kernel growth in CERES-Maize.

In generic models such as WOFOST (Van Diepen et al., 1989) and INTERCOM, growth of plant organs is driven primarily by the availability of assimilates from simulation of canopy photosynthesis, and both growth and maintenance respiration are explicitly accounted for to determine dry matter production. In maize-specific models such as MSB and CERES-Maize, growth of organs is primarily driven by temperature, and dry matter production is computed directly from absorbed solar radiation by means of a fixed value for radiation use efficiency (RUE) that accounts for respiration costs implicitly. Use of a fixed RUE value as the driving force of dry matter accumulation in crop simulation models has been questioned because a fixed RUE value incorporates a number of physiological processes, each of which is sensitive to environmental conditions and crop status (Goudriaan and van Laar, 1994; Loomis and Amthor, 1999). Hence, RUE is a dynamic, integrative variable that is sensitive to temperature and light intensity, and models that rely on a fixed RUE value may be less sensitive to variation in climatic conditions and plant physiological status. For example, Edmeades and Bolanos (2001) speculated that the standard RUE value used in CERES-Maize might be too large for tropical regions where high temperatures may result in greater respiration and high peak radiation intensity is conducive to a reduction in photosynthesis from photo-oxidation.

Models such as CERES-Maize (Carberry et al., 1989; Hodges et al., 1987; Kiniry et al., 1997; Liu et al., 1989; Nouna et al., 2000; Pang et al., 1997; Xie et al., 2001) or MSB (Muchow et al., 1990; Wilson et al., 1995) have been validated extensively against field observations in different environments during the past 15 years. However, the maize yields reported in these validation studies are well below maize yield potential, which is defined as the yield of a crop cultivar when grown in environments to which it is adapted, with nutrients and water non-limiting, and pests and diseases effectively controlled (Evans, 1993). Therefore, most of these validations were based on field experiments in which yields were limited by sub-optimal water or nitrogen (N) supply, or other limiting factors. In addition, most of these studies lack detailed measurements of leaf area index (LAI), phenology, crop biomass, or components of yield. These deficiencies preclude a comprehensive assessment of model performance. To ensure that models are robust...
in simulating yields across the full range of possible yields, it is important to evaluate model performance under high-yield conditions in which yields approach the yield potential ceiling, as well as in environments that produce lower yield levels under stress.

Recent efforts to improve CERES-Maize have focused on leaf area expansion and senescence (Lizaso et al., 2003a), light capture (Lizaso et al., 2003b), and yield components (Ritchie and Alagarswamy, 2003). Although such improvements may lead to improved simulation of specific processes for selected genotypes and environments, they also require additional cultivar-specific input parameters related to leaf characteristics, change of the light extinction coefficient, or kernel set. Widespread use of these more detailed models would likely be limited by the need for additional cultivar-specific input parameters. Moreover, the short lifespan of modern commercial hybrids makes it difficult to utilize detailed models unless the number of cultivar-specific input parameters is small or the parameters can be easily measured and are accessible to end-users.

The objective of our research was to develop a maize model that can simulate maize yield potential and is sensitive to yield potential variation as influenced by solar radiation and temperature regime. The new model, called ‘Hybrid-Maize’, was developed by combining explicit functions for photosynthesis and respiration used in the assimilate-driven generic crop models INTERCOM and WOFOST with revised CERES-Maize formulations for phenological development and organ growth. The Hybrid-Maize model was then evaluated for its ability to simulate maize leaf area expansion, aboveground dry matter accumulation, grain and stover yields in field experiments in which crop management strived to create growth conditions with minimal possible stress from abiotic and biotic factors. For the purpose of comparison, the field experiments were also simulated using CERES-Maize and INTERCOM.

2. Field experiments

2.1. Lincoln, Nebraska

A long-term field experiment was established in 1999 at Lincoln, Nebraska (latitude: 40.82N, longitude: 96.65W, elevation: 357 m a.s.l.) on a deep Kennebec silt loam (fine-silty, mixed, superactive, mesic Cumulic Hapludoll) (Soil Survey Staff, 1999). The purpose of the experiment was to estimate yield potential of maize and soybean under near-optimal growth conditions, and to better understand the crop and soil management factors that determine yield potential.

The 3 × 3 × 2 factorial experiment was arranged in a split–split plot randomized complete block design with four replicates. Crop rotations (continuous maize, maize–soybean, soybean–maize) were main plot treatments, three levels of plant population density were sub-plot treatments (D1, D2, D3), and two levels of fertilizer-nutrient management were sub–subplot treatments (M1: recommended fertilizer rates, M2: intensive nutrient management). Sub–subplots were 6.1 m × 15.2 m in size with eight rows at 0.76 m row spacing. All data presented were obtained in three cropping seasons (1999–2001) from treatments that provided the most favorable growth conditions for high yields: maize grown in rotation with soybean at actual plant densities of 6.9–7.7 plants m⁻² (D1), 8.9–10.2 plants m⁻² (D2), and 11.0–11.3 plants m⁻² (D3), and the M2 intensive nutrient management regime (Table 1).

The crops were irrigated and managed intensively to ensure optimal water and nutrient conditions and avoid stresses from weeds, insects and diseases. The field was deep-ripped in spring 1999 and plowed each year in the fall to create a deep topsoil layer. Average initial soil test values in 0–20 cm depth were pH 5.3, 16 g C kg⁻¹, 67 mg kg⁻¹ extractable P (Bray-1 method), and 350 mg kg⁻¹ 1 M NH₄-acetate extractable K. Lime was applied in 1999 and 2001 to maintain soil pH at about 6.2. Annual nutrient applications to each maize crop were 225–298 kg N ha⁻¹, 45 kg P ha⁻¹, and 85 kg K ha⁻¹. The total N application amount was adjusted each year to account for residual soil nitrate following the University of Nebraska soil testing guidelines. All N was applied as ammonium nitrate. A preplant application of 100–105 kg N ha⁻¹ was incorporated before planting and two to three sidedress doses were applied at V6, V10, and VT stages of maize. Field cultivation was performed at V6 stage to incorporate N fertilizer and control weeds. Blanket doses of S, Fe, and Zn were applied in 1999 and 2000 and omitted in 2001 because...
soil and plant tests indicated adequate supplies of these nutrients. In 1999 and 2000, the experiment was irrigated with a surface drip tape placed beside the plants in each row to fully replenish daily crop evapotranspiration. In 2001, a sub-surface drip irrigation was used with drip tapes placed in alternate rows at a 30 cm depth. Total amount of irrigation was 255 mm in 1999 and 2000, and 540 mm in 2001. Planting dates were 13 May 1999, 21 April 2000, and 26 April 2001. In all 3 years, Bt maize hybrids were used, which minimized the need for insect control with pesticides (Table 1).

2.2. Manchester, Iowa

The Manchester, Iowa site (latitude: 42.47N, longitude: 91.45W, elevation: 302 m a.s.l.) is a farm owned by Francis Childs, winner of the National Corn Growers Association yield contest in recent years (NCGA, 2003). The farm does not have access to irrigation. A description of the site and the cropping practices is provided by Murrell and Childs (2000). In 2002, soil, crop, and daily weather data were collected from four contiguous sampling plots located within a 12 m × 150 m strip of a high-yield field (‘Visitor Plot’) managed by Mr. Childs, following the same management regime applied in his contest-winning field. The field in which our measurements were taken had been in continuous maize with a high-yield management system for more than 20 years, resulting in a significant build-up of soil organic matter in the top 50 cm of soil. The soil is a deep, well-drained Kenyon loam (fine-loamy, mixed, superactive, mesic Typic Hapludoll) formed on uplands in loamy sediments and the underlying glacial till. Soil fertility status was high in the top 50 cm of soil (pH 5.5, 30 g C kg⁻¹, 105 mg kg⁻¹ Bray-1 P, 320 mg kg⁻¹ 1 M NH₄-acetate extractable K in 0–30 cm depth; pH 5.8, 17 g C kg⁻¹, 16 mg kg⁻¹ Bray-1 P, 140 mg kg⁻¹ 1 M NH₄-acetate extractable K in 30–50 cm depth).

Maize hybrid Pioneer 33P67 was planted on 8 May 2002 with a row spacing of 0.51 m and a final plant density of 8.4 plants m⁻². A total of 455 kg N ha⁻¹ was applied, with 56 kg N ha⁻¹ applied in fall, 280 kg N ha⁻¹ knifed in as anhydrous ammonia before planting, 7 kg N ha⁻¹ applied as liquid starter fertilizer at planting, and 112 kg N ha⁻¹ N applied as urea–ammonium nitrate solution shortly after planting. Other nutrient applications included 7.5 kg P ha⁻¹ and 23 kg K ha⁻¹ and various micronutrients (Zn, Fe, Mn, B, Mo) with starter fertilizers. Rainfall was well-distributed throughout the growing season such that crop moisture stress was avoided.

2.3. Measurements

Automatic weather stations located at both field sites provided daily climate data throughout the growing season (Table 2). Plant measurements included the date of major phenological events, aboveground biomass, biomass partitioning (stems, green leaves, dead leaves, reproductive biomass), and LAI at 5 (Manchester) or 7–15 (Lincoln) growth stages. At each sampling time, five consecutive plants were clipped at the soil surface at random locations within each treatment plot at Lincoln and in each of the sampling plots at Manchester.

At physiological maturity (R6 stage), a 6-plant sample was collected from a designated harvest area of 13.9 m² (2 rows × 9.12 m) within each plot to obtain final estimates of biomass partitioning (grain, cobs, stems + leaves) and harvest index (HI). The number of plants, ears, and barren stalks were counted.
within the entire harvest area, and ears were hand-picked to determine grain yield when grain moisture fell below 250 g kg\(^{-1}\). Kernels were separated from cobs, and plant samples were oven-dried to constant weight at 70 °C. All yields are reported on an oven-dry basis. Stover (stems + leaves) and cob dry matter yields were calculated from the grain yield measured in the designated harvest areas and the HI and cob HI obtained from the 6-plant sample collected at the R6 stage.

### 3. Development of the Hybrid-Maize model

The purpose of the Hybrid-Maize model is to accurately predict yield of maize as determined by solar radiation, temperature, phenology, and canopy architecture, when grown under favorable conditions that minimize stress and allow yields to approach yield potential levels. The model includes formulations from CERES-Maize for phenological development and organ growth (Jones and Kiniry, 1986; Kiniry et al., 1997), and functions for photosynthesis and respiration as found in INTERCOM (Kropff and van Laar, 1993) and Goudriaan and van Laar (1994) (Table 3). The modified and new components in Hybrid-Maize that differ from CERES-Maize or INTERCOM are discussed below. Default values of user-modifiable parameters in Hybrid-Maize are listed in Appendix A. Because the functions for crop growth and development in Hybrid-Maize were largely adapted from CERES-Maize, the base temperature of 8 °C in CERES-Maize was retained in Hybrid-Maize for GDD-related internal parameters and variables. For user-input parameters related to GDD, a base temperature of 10 °C is used because most GDD-related crop parameters provided by seed companies are based on this temperature.

Hybrid-Maize is available as a Windows-based PC software with full text and graphical display that allows export of simulation results. The software converts climate data from the High Plains Regional Climate Center (http://www.hprcc.unl.edu) into the format required by the model. It also provides users access to all key model parameters for viewing or editing (Appendix A), as well as the possibility of restoring the original default values of those parameters. The model can be run in single-season mode as well as for long-term simulations using multi-year climate data at a given site. Model source code is available upon request from the senior author (hyang2@unl.edu).

#### 3.1. Light interception and photosynthesis

In CERES-Maize, it is assumed that 50% of the total incident solar radiation (I) is photosynthetically active radiation (PAR). The amount of intercepted PAR (\(\text{PAR}_i\)) by the plant canopy is computed by the exponential function:

\[
\text{PAR}_i = 0.5I(1 - e^{-kLAI})
\]  

and net dry matter production is computed by means of RUE:

\[
\text{DM} = \text{PAR}_i \times \text{RUE}
\]
Table 3
Simulation of major growth and development processes in Hybrid-Maize as compared to CERES-Maize and NTERCOM

<table>
<thead>
<tr>
<th>Processes</th>
<th>CERES-Maize&lt;sup&gt;b&lt;/sup&gt;</th>
<th>INTERCOM&lt;sup&gt;c&lt;/sup&gt;</th>
<th>Hybrid-Maize</th>
</tr>
</thead>
<tbody>
<tr>
<td>Photosynthesis computation</td>
<td>Constant RUE used to directly convert absorbed PAR into DM, adjusted for T; daily time step for PAR interception without regard to solar angle</td>
<td>Total intercepted PAR is split into direct and diffuse parts; solar angle considered; integrated over LAI distribution; adjusted for T</td>
<td>Simplified version of INTERCOM routine, but without splitting total intercepted PAR into direct and diffuse parts and intra-day changes in solar angle</td>
</tr>
<tr>
<td>Maintenance respiration</td>
<td>Not simulated but implicitly ‘discounted’ in the constant RUE value</td>
<td>Based on live biomass and coefficients of 0.03, 0.015, 0.01 and 0.01 g CH₂O respired per gram DM per day for leaf, stem, root and grain respectively, at 25 °C; Q&lt;sub&gt;10&lt;/sub&gt; of 2</td>
<td>Similar to INTERCOM, but with lower coefficients: 0.011, 0.006, 0.006 and 0.005 g CH₂O per gram DM per day for leaf, stem, root and grain, respectively</td>
</tr>
<tr>
<td>Leaf area expansion and senescence</td>
<td>Driven by T as a function of leaf number and assimilate availability; senescence driven by T</td>
<td>Driven by assimilate availability, DM partitioning coefficients, and SLA; partitioning coefficients change with growth stage; senescence driven by T</td>
<td>Similar to CERES-Maize until silking with SLA limited to ( \leq 400 \text{ cm}^2 \text{ g}^{-1} ); leaf senescence after silking modified</td>
</tr>
<tr>
<td>DM accumulation</td>
<td>Driven by T as a function of phenology, limited by assimilate availability; excess assimilate partitioned to roots</td>
<td>Driven by assimilate supply and regulated by DM partitioning to all organs; partitioning coefficients change with growth stage</td>
<td>Similar to CERES-Maize but with modification in dry matter partitioning to root; SLA limited to ( \leq 400 \text{ cm}^2 \text{ g}^{-1} )</td>
</tr>
<tr>
<td>Date of silking</td>
<td>Input parameter, hybrid-specific</td>
<td>Input parameter, hybrid-specific</td>
<td>Either as input parameter or estimated by GDD&lt;sub&gt;silking&lt;/sub&gt; = 100 + 0.4451 GDD&lt;sub&gt;total&lt;/sub&gt; - 50</td>
</tr>
<tr>
<td>Cob growth</td>
<td>Driven by T as a fixed proportion of daily assimilation from silking until GDD = 170 after silking</td>
<td>Simulates mass of whole reproductive organ, including seed and cob</td>
<td>Similar to CERES-Maize but DM partitioning to cob reduced by 60%</td>
</tr>
<tr>
<td>Grain filling and translocation</td>
<td>Filling rate driven by T, assimilate supply and potential filling rate; potential filling rate is hybrid specific; limited translocation from stem and leaf reserves occurs when source &lt; sink with a translocation efficiency of 26%</td>
<td>Filling driven by assimilate supply; amount of translocated assimilate is a fixed proportion of ‘live’ DM loss from stem and leaf senescence</td>
<td>Translocation and grain filling similar to CERES-Maize, actual grain filling rate is adjusted by plant density</td>
</tr>
</tbody>
</table>

<sup>a</sup> RUE, radiation use efficiency; DM, dry matter; T, temperature; PAR, photosynthetically active radiation; LAI, leaf area index; SLA, specific leaf area; GDD, growing degree-days; GDD<sub>silking</sub>, GDD from emergence to silking; GDD<sub>total</sub>, GDD from emergence to maturity.

<sup>b</sup> Jones and Kiniry (1986) and Kiniry et al. (1997).

<sup>c</sup> Kropff and van Laar (1993).
where $I$ is the incoming total solar radiation (MJ m$^{-2}$ per day), $k$ the light extinction coefficient ($= 0.65$ in the original version of CERES-Maize, based on Monteith (1969)), LAI the leaf area index (m$^2$ leaf m$^{-2}$ - ground), and DM the total amount of crop dry matter produced (g m$^{-2}$ ground per day). The value of RUE was set at 5 g MJ$^{-1}$ PAR in the first version of CERES-Maize (Jones and Kiniry, 1986), but reduced to 4.33 g MJ$^{-1}$ PAR in a later version (Kiniry et al., 1997). The 4.33 g MJ$^{-1}$ PAR value was used in the CERES-Maize simulations reported here.

In Hybrid-Maize, PAR$_i$ and gross assimilation are described according to formulations in INTERCOM and WOFOST. The PAR$_i$ and its corresponding CO$_2$ assimilation are computed for each layer in the canopy. Total gross assimilation is then obtained by integration over all layers. Using $L$ to represent the depth of the canopy with $L = 0$ at the top and $L = $ LAI at the bottom of the canopy, the PAR$_i$ at position $L$ in the canopy equals the decrease of PAR at that depth. Differentiation of Eq. (1) yields:

$$\text{PAR}_{i,L} = \frac{d\text{PAR}}{dL} = 0.5k e^{-kL}. \quad (3)$$

where PAR$_{i,L}$ is the PAR interception by the canopy layer at position $L$. The corresponding CO$_2$ assimilation by that layer follows a saturation function of the form:

$$A_L = A_m(1 - e^{-\varepsilon \text{PAR}_{i,L}/A_m}) \quad (4)$$

where $A_L$ is the CO$_2$ assimilation by the canopy layer at $L$, $A_m$ the maximum gross CO$_2$ assimilation rate (g CH$_2$O m$^{-2}$ leaf h$^{-1}$), and $\varepsilon$ the initial light use efficiency (g CO$_2$ MJ$^{-1}$ PAR). The CO$_2$ assimilation by the whole canopy is obtained by integration of Eq. (4) along $L$:

$$A = \int_{L=0}^{\text{LAI}} A_m(1 - e^{-\varepsilon \text{PAR}_{i,L}/A_m}) dL \quad (5)$$

where $A$ is the gross CO$_2$ assimilation of the canopy (g CO$_2$ m$^{-2}$ ground h$^{-1}$). Two numerical integration methods are available in the model. The default method, which was used in all the simulations of this study is the three-point Gaussian method (Goudriaan, 1986). Alternatively, a user can choose the standard Simpson’s rule with a user-defined precision. A $k$ value of 0.55 is used in Hybrid-Maize based on data from Lizaso et al. (2003b), Maddonni et al. (2001), and our measurements made in the field experiment at Lincoln (J.L. Lindquist, unpublished data). The values of $\varepsilon = 12.5$ g CO$_2$ MJ$^{-1}$ PAR, $A_m = 7$ g CO$_2$ m$^{-2}$ leaf h$^{-1}$, and the relationship of $A_m$ with temperature were adapted from Kropff and van Laar (1993). Unlike INTERCOM, Hybrid-Maize computes the gross assimilation in a daily time step without differentiating incident radiation into diffuse and direct components.

### 3.2. Maintenance and growth respiration

CERES-Maize uses RUE to convert PAR$_i$ directly into dry matter production and, therefore, does not explicitly account for growth or maintenance respiration. Hybrid-Maize utilizes formulations for maintenance and growth respiration similar to those in INTERCOM, and the coefficients of growth respiration for leaf, stem, root and grain (Table 3) were adopted from Penning de Vries et al. (1989), as used by Kropff and van Laar (1993). Similar to INTERCOM and WOFOST, Hybrid-Maize assumes that the entire mass of each organ respires before silking, but only the ‘live’ biomass thereafter. The fraction of ‘live’ biomass after silking is set to be equal to the ratio of LAI at any point during grain filling to the maximum LAI, which occurs at silking (Kropff and van Laar, 1993). Maintenance respiration of each organ is then estimated on a daily time step as a fraction of live biomass.

The coefficients for maintenance respiration (MRC) used in generic crop models such as INTERCOM were derived nearly two decades ago, based on a combination of theoretical considerations, experimental measurements, and model studies (Penning de Vries et al., 1989; van Ittersum et al., 2003). These coefficients may be too large for modern maize hybrids. Earl and Tollenaar (1998) showed that more recent maize hybrids had smaller respiration losses than older hybrids. Therefore, the MRC coefficients for maintenance respiration in Hybrid-Maize were obtained by calibrating model prediction of dry matter yields against the observed yields from the field experiment conducted in 1999 at Lincoln (Table 3). No other experimental data were used for this calibration. Smaller MRC coefficients than those used in generic crop models such as INTERCOM greatly improved the accuracy of predicting dry matter accumulation. Moreover, the mean of the MRC obtained from this
calibration (0.007 g g\(^{-1}\) per day) was comparable to the whole-plant respiration value of 0.008 g g\(^{-1}\) per day at silking reported by Kiniry et al. (1992).

3.3. Leaf growth and senescence

In CERES-Maize, temperature drives leaf area expansion, which in turn drives leaf biomass growth as follows:

\[
LW = \left( \frac{PLA}{267} \right)^{1.25} \tag{6}
\]

where LW is the total leaf biomass (g per plant), and PLA the total plant leaf area (cm\(^2\) per plant). According to Eq. (6), the specific leaf area (SLA) will exceed 400 cm\(^2\) g\(^{-1}\) at PLA of 50 cm\(^2\) per plant, and exceed 300 cm\(^2\) g\(^{-1}\) at PLA of 165 cm\(^2\) per plant. However, in the field experiments at Lincoln with maize grown under optimal conditions, SLA never exceeded 300 cm\(^2\) g\(^{-1}\) (J.L. Lindquist, unpublished data), which is also in agreement with the observations of Kropff et al. (1984). This suggests that CERES-Maize may under-predict leaf biomass growth during the early vegetative stage. Therefore, a limit of SLA \(\leq 400\) cm\(^2\) g\(^{-1}\) was set in Hybrid-Maize when estimating leaf biomass growth from leaf area expansion, and SLA was computed at the end of each day as:

\[
SLA = \frac{LW}{PLA} \tag{7}
\]

In CERES-Maize, leaf area expansion ceases at silking, which is the point of maximum LAI, and leaf senescence proceeds thereafter in two phases. The first phase, from start of silking to beginning of effective grain filling, lasts for 170 GDD and follows:

\[
SLAN = PLA_{\text{silking}} \times 0.05 \left(1 + \frac{\text{sumDTT}}{170}\right) \tag{8}
\]

where SLAN denotes the total senescent leaf area (cm\(^2\) per plant), PLA\(_{\text{silking}}\) the total leaf area at silking (cm\(^2\) per plant), sumDTT the cumulative GDD from the start of silking. The second phase proceeds from the beginning of effective grain filling until maturity according to:

\[
SLAN = PLA_{\text{silking}} \left(0.1 + 0.8 \left(\frac{\text{sumDTT}}{P_5}\right)^3\right) \tag{9}
\]

where \(P_5\) is the GDD from silking to maturity. The SLAN estimated by Eqs. (8) and (9) is then compared with the total leaf senescence that would occur from low light intensity (i.e. lack of light in the bottom layers of the canopy) and low temperature, as estimated by specific formulations for these effects, and the smaller of the two estimates is then taken as the actual leaf senescence. The drawbacks of this approach are the abrupt decreases in LAI at the onset of silking and at the transition from linear senescence (Eq. (8)) to rapidly accelerated leaf senescence thereafter (Eq. (9))—patterns that not observed in the field.

In Hybrid-Maize, the two phases of leaf senescence were combined into one function for leaf senescence for the whole period from start of silking to maturity:

\[
SF = 0.7 \left(\frac{\text{sumDTT}}{P_5}\right)^4 \tag{10}
\]

in which SF denotes the senescent leaf area as a fraction of LAI at silking. The sumDTT is calculated as:

\[
\text{sumDTT} = \frac{\text{sumDTT} + \text{DTT}}{1 - \text{LSR}} \tag{11}
\]

in which DTT denotes the daily effective temperature, LSR the stress rate caused by low temperature and competition for light (0 to 1, with 1 for stress free and 0 for full stress, as in CERES-Maize). In Eq. (10), the exponent, or stay-green coefficient, determines the speed of leaf senescence while the coefficient 0.7 determines the final amount of senescent LAI as a fraction of maximum LAI at silking. Both parameters are related to the ‘stay-green’ trait of maize hybrids as well as G \(\times\) E interactions that influence leaf senescence, especially with regard to plant N status and water relations (Fakorede and Mock, 1980; Rajcan and Tollenaar, 1999). Although commercial seed companies typically provide scores for the stay-green trait, the scale differs among individual companies because the scores are not based on a standardized scale. While the current version of Hybrid-Maize, as used in this study, treats the exponent and coefficient in Eq. (10) as constants, it would be possible to treat them as dynamic variables responsive to N and water stress, or as hybrid-specific input parameters.
3.4. Development stages and occurrence of silking

In CERES-Maize, aboveground phenological development is divided into five stages marked by six indicators: emergence, end of juvenile phase, tassel initiation, silking, start of effective grain filling, and physiological maturity. The duration of the first stage (from emergence to end of juvenile phase) is determined by the input parameter $P_1$, which is the GDD requirement for this growth period. The duration of the second stage (from end of juvenile phase to tassel initiation) is a function of the input parameter $P_2$, or the photoperiod sensitivity, and the latitude of the field site. The functions governing plant growth and development are the same in stage-1 and stage-2. The duration of stage-3 (from tassel initiation to silking) is a proportional function of the accumulated GDD of the first two stages. The duration of stage-4 (from silking to the start of effective grain filling) is fixed at GDD = 170, and the duration of the fifth and final stage is determined by the input parameter $P_5$, which is the GDD from silking to maturity.

Occurrence of silking has a large influence on simulated grain yield through the effect on length of grain filling. In CERES-Maize, silking is determined by the input parameters $P_1$ and $P_2$. It is difficult, however, to estimate the value of $P_1$ under field conditions (Edmeades and Bolanos, 2001), and $P_1$ is not readily available for most commercial hybrids grown in different environments. Moreover, it is not known if $P_1$ is a constant for hybrids with similar maturity, or if it is sensitive to environmental conditions other than temperature. This uncertainty makes the selection of an appropriate $P_1$ difficult, which could result in inaccurate prediction of silking (Roman et al., 2000). Overall, CERES-Maize requires input of three hybrid-specific input parameters ($P_1$, $P_2$, and $P_5$) to simulate aboveground phenological development.

In contrast, Hybrid-Maize requires only one hybrid-specific parameter to simulate aboveground phenological development as defined by tassel initiation, silking, grain filling and physiological maturity. Occurrence of silking is determined in one of two ways: (1) by user input of GDD from emergence to silking ($\text{GDD}_{\text{silking}}$, base $T = 10 ^\circ \text{C}$), or (2) by user input of total GDD from emergence to maturity ($\text{GDD}_{\text{total}}$, base $T = 10 ^\circ \text{C}$). Many seed companies typically publish $\text{GDD}_{\text{silking}}$ or $\text{GDD}_{\text{total}}$ values for their commercial hybrids, which means that one or both parameters are generally available. In some cases, however, only one of these two parameters is available. In such cases, Hybrid-Maize estimates either $\text{GDD}_{\text{silking}}$ or $\text{GDD}_{\text{total}}$ from the following relationship (Fig. 1):

$$\text{GDD}_{\text{silking}} = 100 + 0.445 \text{GDD}_{\text{total}}$$ (12)
This relationship was derived from published values of GDD\text{silking} and GDD\text{total} for 107 commercial maize hybrids that are widely used in the north-central USA (Pioneer Hi-Bred, 2001). However, in Hybrid-Maize, an additional offset of $-50$ was applied to the intercept in Eq. (12) to provide a more accurate prediction of silking under optimal water conditions. This offset was included because the data sets used to obtain the relationship in Eq. (12) came from thousands of field trials conducted under a wide range of growth conditions that included both irrigated and rainfed environments. Under such widespread testing, some of the rainfed sites experience a water deficit, which delays silking (Saini and Westgate, 2000). Therefore, the GDD\text{silking} under optimal irrigated conditions would likely be smaller than the average of values obtained from widespread testing.

After establishing GDD\text{silking}, the occurrence of tassel initiation in Hybrid-Maize is then determined by an iterative process from CERES-Maize that utilizes a proportional function relating the duration from tassel initiation to silking to the duration of the first two development stages.

### 3.5. Cob growth and grain filling

In CERES-Maize, cob growth is initiated at silking with initial biomass set to equal 17% of total stem biomass, and cob growth ceases at the end of stage-4 when effective grain filling begins. When calibrated against measurements in the Lincoln field study, however, the predicted cob biomass was double the measured values. Therefore, in Hybrid-Maize, the daily dry matter allocation to cob was reduced by 60% compared to CERES-Maize.

The daily grain-filling rate in CERES-Maize is the product of the potential grain-filling rate ($G_5$) and the grain filling efficiency, which is driven by temperature but is independent of plant density. As a result, simulated weight of individual grains is constant across large differences in plant density. Typically, individual grain weight decreases in cereal crops as plant density increases, especially at high plant populations. Using 1999 and 2000 data from the three plant density treatments at Lincoln, the following empirical relationship was derived and used in Hybrid-Maize to reduce the rate of grain filling at increased plant densities:

$$ F = 1.47 - 0.09D + 0.0036D^2, \quad r^2 = 0.78, P < 0.01 $$

(13)

where $F$ denotes the factor for adjusting grain filling rate based on plant population ($D$, plant m$^{-2}$). Because Eq. (13) was derived for a range of $6.9–11.3$ plants m$^{-2}$, the value of $F$ was limited to $\geq 0.89$ and $\leq 1.0$ in the model. While plant densities for irrigated maize typically fall within this range, the relationship in Eq. (13) has not been validated at higher or lower densities and therefore the model should not be used outside this range.

### 3.6. Root biomass

In CERES-Maize, root growth is divided into the three stages from stage-1 to stage-3, and stops at end of stage-3. Each of these stages has a minimum dry matter partitioning fraction to roots: 0.25, 0.1 and 0.08 for stage-1, stage-2 and stage-3, respectively. Any dry matter in excess of growth requirements for leaves and stems is partitioned to roots on a daily time step. In addition, half of the gross gain of dry matter allocation to roots is lost to respiration, and 0.5% of the total root biomass is lost via root senescence—both on a daily time step.

In Hybrid-Maize, a continuous function derived from the data for maize in Kropff and van Laar (1993), was used to determine the minimum fraction of dry matter partitioning to roots ($RF_{\text{min}}$):

$$ RF_{\text{min}} = 0.35 - \frac{0.35 \text{GDD}}{1.15 \text{GDD}_{\text{silking}}}, \quad RF \geq 0 $$

(14)

where GDD denotes the growing degree-day accumulation from emergence. If there is dry matter remaining after meeting the growth requirements for leaf and stem and $RF_{\text{min}}$, the dry matter fraction partitioned to roots is increased to an upper limit of 0.5 of daily net assimilation. Moreover, all the dry matter gain in root is treated as a net gain in plant dry matter because respiration is already accounted for in the estimation of net assimilation. Allocation of dry matter to roots ceases when GDD reaches 115% of GDD\text{silking}. Similar to CERES-maize, 0.5% of the root biomass is lost via fine-root turnover or senescence on a daily basis.
3.7. Model evaluation and sensitivity analysis

The performance of Hybrid-Maize was evaluated for all 10 data sets listed in Table 1, including nine year × plant density treatment combinations at Lincoln and the 2002 growing season at Manchester. All simulations were initiated from emergence, and the actual GDD_{total} of the four cropping seasons was used as an input parameter such that simulations terminated on the dates of observed physiological maturity (Table 1). Measured plant densities were also used, and silking was predicted for each growing season by Eq. (12) based on GDD_{total}. Values of the other key parameters in Hybrid-Maize are given in Appendix A.

The 10 data sets were also simulated with CERES-Maize (1995 version provided by J. Kiniry) and INTERCOM (Lindquist, 2001). For CERES-Maize, each simulation was initiated from the date of sowing and the sowing depth was adjusted so that the predicted date of emergence matched the observed date. Parameters $G_2$ and $G_5$ were set the same as the values used in Hybrid-Maize (Appendix A). For each run, $P_5$ was set so that the simulation ended on the date of observed maturity. For Lincoln 1999 and 2000 and Manchester, $P_1$ was set at 220, which is the mean $P_1$ value for northern and southern Nebraska, Iowa, Illinois and Indiana (Jones and Kiniry, 1986). For Lincoln 2001, $P_1$ was set at 250 because the observed date of maturity could not be reached even when $P_5$ was set at 999 (the highest value the CERES-Maize program accepts). For INTERCOM, all runs started from the date of observed emergence. Development rates for vegetative and reproductive stages were input parameters based on the inverse of actual GDD (base $T = 10^\circ C$) in each season from emergence to silking and from silking to maturity, respectively. Because INTERCOM does not simulate cob and grain growth separately, grain yield was estimated to be 87% of the total ear biomass based on grain to ear mass ratio measured in the Lincoln experiment. For both CERES-Maize and INTERCOM, simulations were performed with settings for optimal water and nutrient supply.

The degree of agreement between simulated and measured values for LAI and dry matter accumulation were assessed in two ways. The first plots the absolute value of the difference between predicted and measured values for LAI and dry matter accumulation versus the day after emergence when the measurements were made to examine whether the models have a particular bias during specific growth stages. The second quantifies the deviations between predicted and measured values by estimating the modeling efficiency (EF) and absolute modeling error (AE), as computed by (Smith et al., 1997):

$$\text{EF} = 1 - \frac{\sum_{i=1}^{n} (P_i - O_i)^2}{\sum_{i=1}^{n} (O_i - \bar{O})^2}$$

where $O_i$ denotes measured values, $\bar{O}$ the mean of $O_i$, $P_i$ the predicted values, and $n$ the number of measurements. As EF is similar to $r^2$ in regression analysis, $\text{EF} = 1$ indicates perfect agreement of model predictions with the direct measurements of the parameter in question, and $\text{EF} = 0$ or a negative EF indicates that $\bar{O}$ is a better predictor than the model. Absolute error (AE) is an indicator of the mean bias in the total difference between simulated values and measurements:

$$\text{AE} = \frac{1}{n} \sum_{i=1}^{n} (P_i - O_i)$$

Hence, $\text{AE} < 0$ indicates under-prediction and $\text{AE} > 0$ indicates over-prediction. The AE corresponding to the 95% confidence interval of the two-tailed $t$-test ($\text{AE}_{95\%}$) was computed by:

$$\text{AE}_{95\%} = \frac{1}{n} \sum_{i=1}^{n} (t_{(n-2)95\%} \times \text{S.E.})$$

where $t_{(n-2)95\%}$ denotes the two-tailed $t$ at 95% interval with d.f. = $n - 2$ and S.E. is the standard error of the mean. The AE becomes significant if $\text{AE}_{95\%}$. Because fewer dry matter measurements were taken after silking when dry matter values and associated simulation errors are much larger than in the vegetative stage, the EF and AE values should be interpreted with caution.

The Hybrid-Maize model was also tested for the sensitivity of maize yield potential to selected parameters from Appendix A using 17 years of weather data (1986–2002) at Lincoln. The following parameters were evaluated: the two hybrid-specific coefficients related to kernel set and grain filling ($G_2$ and $G_5$), light extinction coefficient ($k$), translocation efficiency (TE) of carbohydrate for grain filling, initial light use efficiency ($\psi$), MRC of leaf, stem, root and
4. Results

4.1. Simulation of maize growth dynamics with minimal stress

Climatic conditions in the 2000 and 2001 growing seasons at Lincoln differed substantially from those in 1999 (Table 2). The crop was sown later in 1999 than in 2000 and 2001 so that vegetative growth was reduced and grain filling occurred in late August and early September in 1999, when the minimum (night) temperature seldom exceeded 21 °C. In contrast, earlier planting in both 2000 and 2001 and relatively hot and dry periods in July and August caused grain filling to occur with mean minimum air temperature exceeding that of 1999 by 1.4–1.8 °C. Consequently, the grain filling periods in 2000 and 2001 were 9 and 2 days shorter than in 1999, respectively. At Manchester, cumulative solar radiation during the entire growing season was similar to that of 1999 and 2000 at Lincoln, but crop maturity occurred later due to a much longer grain filling period (65 days). The longer grain filling period at Manchester was associated with a mean maximum temperature that was 3–4 °C cooler than that at Lincoln, while mean minimum temperature was 5–7 °C cooler during grain filling.

Simulated LAI by all three models was in close agreement with observed values for the first 30 or 40 days after emergence (Figs. 2–4). At later development stages, simulated LAI values were more accurate at low plant density than at high plant density, but all models tended to under-predict maximum LAI during mid-season (Fig. 3), particularly when measured LAI was >6. LAI remained near maximum levels for about 40 days after silking, which indicates active canopy assimilation during grain filling and lack of stress from inadequate water or N supply. Overall, predictions of

<table>
<thead>
<tr>
<th>Model (site-year)</th>
<th>Modeling efficiency (EF)</th>
<th>Absolute error (AE)(^a)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>LAI</td>
<td>AG biomass</td>
</tr>
</tbody>
</table>

Hybrid-Maize
- Lincoln 1999: 0.93, 0.99; 0.22 ns, 0.27 ns
- Lincoln 2000: 0.88, 0.97; -0.32 ns, 0.50 ns
- Lincoln 2001: 0.90, 0.98; -0.56\(^c\), -0.27 ns
- Manchester 2002: 0.90, 1.00; -0.42 ns, -0.09 ns

CERES-Maize
- Lincoln 1999: 0.90, 0.95; 0.08 ns, -0.38 ns
- Lincoln 2000: 0.69, 0.97; -0.76\(^c\), -0.27 ns
- Lincoln 2001: 0.63, 0.95; -1.16\(^c\), -0.87 ns
- Manchester 2002: 0.82, 0.98; -0.67\(^c\), -0.99 ns

INTERCOM
- Lincoln 1999: 0.71, 0.87; -0.67\(^c\), -1.26 ns
- Lincoln 2000: 0.90, 0.95; -0.34 ns, -0.46 ns
- Lincoln 2001: 0.50, 0.80; -1.52\(^c\), -2.92\(^c\)
- Manchester 2002: 0.43, 0.89; -1.54\(^c\), -2.41\(^c\)

\(^a\) Values for Lincoln 1999–2001 are based on observations from the three plant density treatments.

\(^b\) ns indicates an AE value smaller than the 95% confidence interval in two-tailed t-test with d.f. = n – 2.

\(^c\) Indicates an AE value corresponding to a 95% confidence interval in two-tailed t-test with d.f. = n – 2.
LAI dynamics by Hybrid-Maize were closer to measured values than LAI simulated by CERES-Maize or INTERCOM (Table 4). Leaf senescence simulated by CERES-Maize proceeded too quickly, which resulted in a much smaller LAI than observed throughout the grain filling period. Both CERES-Maize and INTERCOM were less consistent in predicting LAI patterns in different years, which is captured by widely varying EF values across years. Substantial under-prediction of LAI by these two models was also indicated by significant and large negative AE values in most site-years, particularly in 2001 at Lincoln. In contrast, Hybrid-Maize EF values for LAI were closer to one and the AE values were significant in only one out of four cases—an indication of significant improvement in the prediction of LAI changes during the growing season across plant densities and years.

All three models were capable of predicting early season aboveground dry matter, but they differed in their prediction of biomass after silking (Figs. 4–6). In general, Hybrid-Maize closely predicted total aboveground dry matter after silking at both sites and at all plant densities, whereas both CERES-Maize and INTERCOM consistently under-predicted dry matter accumulation during the reproductive phase. Modeling efficiencies for total biomass by Hybrid-Maize ranged from 0.97 to 1.00 and the AE was not significant in any of site-years evaluated (Table 4). The short periods of simulated decreases in dry matter accumulation after silking in Hybrid-Maize and CERES-Maize result from the periods of low light intensity or high temperatures when daily requirements for grain filling are not met by net assimilation and translocation of stem carbohydrate reserves makes up the difference (Kiniry et al., 1992).

Fig. 2. Observed (symbols and error bars = mean and S.E.) LAI of maize and LAI predicted by Hybrid-Maize (fine line), CERES-Maize (medium line), and INTERCOM (thick line) for three plant density treatments (D1, D2, and D3) at Lincoln during 1999–2001. Actual plant densities are shown at upper left of each panel, and vertical bars along the x-axis indicate the date of silking.
4.2. Prediction of grain yield, final stover biomass, and HI

Observed grain yields in the plant density treatments at Lincoln ranged from 12.5 to 14.0 Mg ha\(^{-1}\) on an oven-dry basis (Table 5). Grain yields simulated by Hybrid-Maize were \(-5\) to \(+12\%\) of the measured yields across treatments and years. The maximum grain yield measured in the highest-yielding replicate plot may serve as an estimate of the climatic-genetic yield potential at the Lincoln site for the years in which the study was conducted. Maximum plot yields were 14.4 Mg ha\(^{-1}\) in 1999 (in a plot with 11.4 plants m\(^{-2}\)), 14.0 Mg ha\(^{-1}\) in 2000 (in a plot with 9.8 plants m\(^{-2}\)), and 14.5 Mg ha\(^{-1}\) in 2001 (in a plot with 11.2 plants m\(^{-2}\)). These maximum measured yields are in close agreement with the yield potential simulated by Hybrid-Maize of 14.3, 14.0, and 14.1 Mg ha\(^{-1}\) for these same treatment–year combinations (Table 5). The model was also relatively robust in accounting for differences in grain yield associated with plant density in most years. The largest discrepancy between measured and simulated grain yield occurred at the highest plant density in 2000, when measured yield at 11.0 plants m\(^{-2}\) (12.5 Mg ha\(^{-1}\)) was smaller than that at a density of 9.6 plants m\(^{-2}\) (13.6 Mg ha\(^{-1}\)). In that year, unusually high temperatures in the second half of grain filling

![Graph showing deviation of LAI calculated as predicted minus observed values for three plant densities (D1, D2, and D3) at Lincoln during the 1999–2001 cropping seasons.](image)
Fig. 4. Observed (symbols and error bars = mean and S.E.) and simulated LAI and total aboveground biomass of maize at Manchester, 2002. Simulated values are shown for Hybrid-Maize (thin line), CERES-Maize (medium line) and INTERCOM (thick line) models. The vertical bar along the x-axis indicates the date of silking. Plant population was 8.4 plant m$^{-2}$.

Table 5
Measured (M) and simulated grain and stover yields, and HI by Hybrid-Maize (HM), CERES-Maize (CM), and INTERCOM (I) at Lincoln (1999–2001) and Manchester$^a$

<table>
<thead>
<tr>
<th>Site–year</th>
<th>Plants m$^{-2}$</th>
<th>Grain dry matter (Mg ha$^{-1}$)</th>
<th>Stover dry matter (Mg ha$^{-1}$)</th>
<th>HI</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>M</td>
<td>HM</td>
<td>CM</td>
</tr>
<tr>
<td>Lincoln 1999</td>
<td>7.0</td>
<td>12.8 (0.2)</td>
<td>12.6</td>
<td>10.6</td>
</tr>
<tr>
<td></td>
<td>8.9</td>
<td>13.4 (0.2)</td>
<td>13.5</td>
<td>11.8</td>
</tr>
<tr>
<td></td>
<td>11.3</td>
<td>14.0 (0.1)</td>
<td>14.3</td>
<td>12.7</td>
</tr>
<tr>
<td>Lincoln 2000</td>
<td>6.9</td>
<td>12.5 (0.3)</td>
<td>12.0</td>
<td>11.9</td>
</tr>
<tr>
<td></td>
<td>9.6</td>
<td>13.6 (0.3)</td>
<td>13.4</td>
<td>13.2</td>
</tr>
<tr>
<td></td>
<td>11.0</td>
<td>12.5 (0.3)</td>
<td>14.0</td>
<td>13.8</td>
</tr>
<tr>
<td>Lincoln 2001</td>
<td>7.7</td>
<td>13.4 (0.3)</td>
<td>12.7</td>
<td>12.2</td>
</tr>
<tr>
<td></td>
<td>10.2</td>
<td>13.8 (0.1)</td>
<td>13.8</td>
<td>13.5</td>
</tr>
<tr>
<td></td>
<td>11.2</td>
<td>13.6 (0.3)</td>
<td>14.1</td>
<td>13.9</td>
</tr>
<tr>
<td>Manchester 2002</td>
<td>8.4</td>
<td>13.5 (0.1)</td>
<td>14.7</td>
<td>13.7</td>
</tr>
<tr>
<td>Overall mean</td>
<td>13.3</td>
<td>13.5 (0.27)</td>
<td>12.7</td>
<td>9.9</td>
</tr>
</tbody>
</table>

$^a$ Values in parentheses are standard errors.
caused a large decrease in the grain filling period. For example, the grain filling period from silking to physiological maturity was 45 days in 2000 compared to 54–52 in 1999 and 2001 (Table 1), and it appears that Hybrid-Maize was not sensitive to the effects of these high temperatures on grain yield at high plant density.

Predictions of stover yield and HI by Hybrid-Maize were also in reasonable agreement with observed values for most year × plant density treatment combinations at Lincoln (Table 5). The greatest disagreement between predicted and measured values for stover biomass occurred at the highest plant population in 2000 and 2001 when temperatures during the reproductive phase were well above the 17-year mean for the Lincoln site (Table 2). We suspect that increased respiration losses associated with above-average temperatures during grain filling and high plant density may have reduced biomass, and this interaction is not fully accounted for by Hybrid-Maize. At Manchester, measured grain and stover yields were similar to yields at Lincoln, and the yield potential and HI simulated by Hybrid-Maize was in close agreement with measured values at this site (Table 5).

Yields and HI simulated by Hybrid-Maize were in closer agreement with measured values than simulations by CERES-Maize or INTERCOM when evaluated across all sites, years, and density treatments (Table 5). The improvement in simulation accuracy was especially notable for stover yields, for which simulations by CERES-Maize and INTERCOM averaged 18 and 28% less than measured yields.

4.3. Sensitivity analyses

Under growth conditions with minimal stress, total biomass yield simulated by Hybrid-Maize was most sensitive to changes in the initial light use efficiency ($e$) (Fig. 7a). Changes in the other plant traits had relatively little effect on total biomass yield. Grain yields were sensitive to changes in potential sink size ($G_2$), potential grain filling rate ($G_5$), and $e$, all of which increased yield with increasing values.
Grain yields were also very sensitive to time of silking, which highlights the importance of accurate specification or estimation of GDD$_\text{silking}$ to obtain reliable estimates of grain yield from maize simulation models.

The predicted grain yield and aboveground biomass for each of the scenarios in the sensitivity simulations were remarkably stable across the 17 years of climate data. For example, the standard error for the magnitude of difference in total biomass and grain yield simulated over 17 years for each of the modified scenarios in Fig. 7 ($n = 84$) was less than 1% in all but three cases. This stability suggests that typical year-to-year variation in climate has relatively small effects on the sensitivity of the parameters tested.

5. Discussion

The need for a model that can provide robust simulation of maize yield potential in different environments with a minimum number of location- or hybrid-specific input parameters was the motivation for developing Hybrid-Maize. Agronomists need such robust crop models to improve the efficiency of research that investigates interactions among crop management options in favorable rainfed and irrigated environments, while crop producers and crop consultants need such models for use in computer-based decision-support tools to improve crop management decisions.

The Hybrid-Maize model builds on the strengths of existing models by combining the crop-specific attributes of CERES-Maize related to phenology and grain filling with explicit photosynthesis and respiration functions from generic crop models such as INTERCOM. Hybrid-Maize also includes additional modifications for several functions based on calibration with experimental data from a field study that produced maize with minimal possible stress conditions that are required to achieve yield potential. When validated against measured yields that approach yield potential...
levels, Hybrid-Maize simulated seasonal patterns of LAI and dry matter accumulation, final yields of grain and stover, and HI more accurately than the models from which it was derived. In addition, Hybrid-Maize required fewer cultivar-specific parameters than CERES-Maize, and those parameters are readily available for most commercial varieties.

Accurate prediction of time to silking is crucial for reliable prediction of grain yield, as documented in the sensitivity analysis. A unique feature of Hybrid-Maize is the ability to predict time of silking based on the GDD_total for a given hybrid, which is likely to improve modeling applications that require forecasting rather than post-season analysis. In contrast, CERES-Maize requires two input parameters ($P_1$ and $P_2$) to predict silking, and both parameters are difficult to measure and are not available for most commercial hybrids. For the four cropping seasons simulated in this study, Hybrid-Maize predicted silking within $\pm 3$ to $+1$ days from the actual day of silking while CERES-Maize consistently under-predicted silking by $-3$ to $-6$ days.

As a new model, Hybrid-Maize has not been evaluated widely and it remains to be seen how well it can predict maize yield potential across a greater range of environments than evaluated in our study. Despite the encouraging results from the validations reported here, some discrepancies were apparent between model predictions of yield potential and measured yields under field conditions, particularly at high plant density and high temperatures during grain filling. In most cases, the maximum LAI at high plant density was

![Fig. 7. Sensitivity analysis of the Hybrid-Maize model based on 17-year mean weather data (1986–2002) at Lincoln. Parameters tested were potential number of kernels per ear ($G_2$), potential kernel filling rate ($G_5$), light extinction coefficient ($k$), CH₂O translocation efficiency (TE), initial light use efficiency ($e$), mean maintenance respiration coefficient (MRC), and occurrence of silking (day of silking). Except for day of silking, the changes in parameter were $\pm 10\%$, $\pm 20\%$ and $\pm 30\%$ of the default values listed in Table 4. The changes for day of silking were $\pm 2$, $\pm 5$ and $\pm 10$ days. Each point represents the mean relative change in simulated yields across the 17-year simulation compared to the simulated yields using the default values. Plant density was set 10 plants m$^-2$ and total GDD from emergence to maturity was set at 1500, which is typical of hybrids used in the field studies.](image-url)
consistently under-predicted by all three models, which indicates that the description of leaf area expansion is still not sufficiently robust when plant densities exceed 9 plants m\(^{-2}\). Because a larger LAI implies greater C and N requirements for growth, higher maintenance respiration costs, and a larger N storage capacity, under-prediction of LAI could potentially affect the accuracy of simulating C and N translocation and leaf senescence rates during grain filling.

Hybrid-Maize has not been tested in stress environments where crop growth is limited by water stress, nutrient deficiencies, or both. In such stress environments, under-prediction of LAI would likely have a much larger impact on simulated yields than under the optimal growth conditions of the field experiments used to validate simulations in our study. In Hybrid-Maize, canopy leaf area is simulated by a discontinuous set of equations as in the original CERES-Maize model: one for the period before tassel initiation and another for the period thereafter to silking (Jones and Kiniry, 1986). This approach provides few opportunities to account for genotypic differences in leaf expansion and senescence or to simulate the interactive effects of stresses on these processes (Lizaso et al., 2003a), and such interactions were identified as constraints to accurate prediction of maize growth under stress conditions (Carberry et al., 1989; Keating et al., 1992). We therefore expect that the functions describing leaf expansion during rapid vegetative growth in Hybrid-Maize will need improvement if the model is to be used for simulation of maize growth in stress environments. While Lizaso et al. (2003a) have proposed a more detailed, cultivar-specific leaf area model for maize, it requires three additional cultivar-specific input parameters related to leaf growth and expansion.

All three models showed a lack of agreement between predicted and measured yields at high plant density in years with higher than normal temperatures during grain filling. The interactive effects of plant density and temperature on gross assimilation and assimilate loss from maintenance respiration are apparently not well-accounted for in these models. Addressing this deficiency will require experimental data on respiration costs of different organs at different development stages under a representative range of temperatures and plant density (van Ittersum et al., 2003). Recent proposed revisions of CERES-Maize have focused on genotype and plant density effects on prolificacy, barrenness, and kernel number (Ritchie and Alagarswamy, 2003). Although these modifications improved the prediction of grain yield and yield components, effects on predicted stover biomass and HI were not reported and obtaining the three additional hybrid-specific genetic coefficients would be a major obstacle for use of such models.

Hybrid-Maize uses a default value of 12.5 g CO\(_2\) MJ\(^{-1}\) PAR from Kropff and van Laar (1993) for the initial light use efficiency \(\varepsilon\) (Appendix A). Although the sensitivity analysis identified \(\varepsilon\) as a sensitive parameter influencing dry matter production, the range of \(\varepsilon\) evaluated in Fig. 7 (9–16 g CO\(_2\) MJ\(^{-1}\)) was far greater than the narrow variation in \(\varepsilon\) found in C4 crops like maize (Ehleringer and Pearcy, 1983; Loomis and Amthor, 1999). Given this lack of variation, prospects for further model improvement through more accurate measurement and specification of \(\varepsilon\) appear to be small.

Like CERES-Maize, Hybrid-Maize also simulates root biomass yield and root turnover. This component of Hybrid-Maize has not been validated against experimental data for partitioning of assimilates belowground, and we are not aware of validation studies of this component in CERES-Maize. In fact, such validation represents a substantial experimental effort because assimilate partitioned belowground contributes to root growth, root turnover, root respiration, and root exudation. Hence, a full accounting of belowground root carbon under field conditions is a difficult, and labor-intensive task.

Our longer term goals are to utilize Hybrid-Maize for three purposes: (1) to better understand maize yield potential per se and the effects of climate on yield potential, (2) to improve estimates of C inputs to soil from maize residues and roots to simulate the C sequestration potential of irrigated maize systems, and (3) to develop a decision-support software tool that includes simulation of maize yield potential to help producers and crop consultants improve crop management decisions regarding hybrid selection, date of planting, plant density, and N fertilizer management in high-yield production environments. While validation across a wider range of environments will be required to provide a more rigorous test of Hybrid-Maize, it appears to have some advantages over existing models in simulating maize yield potential under the favorable growth conditions of the field sites in this
study. In addition, Hybrid-Maize gave more accurate simulations of HI and final stover yield, which are critical parameters for simulating C inputs to soil from crop residues and subsequent C sequestration.

Acknowledgements

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### Appendix A

User-modifiable parameters, their default values and references in the Hybrid-Maize model

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Default value</th>
<th>Reference</th>
</tr>
</thead>
<tbody>
<tr>
<td>Potential number of kernels per ear ($G_2$). The default value is for high yielding maize hybrids in the High Plains of US</td>
<td>675 kernels per ear</td>
<td>Mean of the cultivars for northern and southern Nebraska, Iowa, Illinois and Indiana in Table 3.4 of Jones and Kiniry (1986)</td>
</tr>
<tr>
<td>Potential kernel filling rate ($G_5$). The default value is for high yielding maize hybrids in the High Plains of US</td>
<td>8.7 mg kernel$^{-1}$ per day</td>
<td>Mean of the cultivars for northern and southern Nebraska, Iowa, Illinois and Indiana in Table 3.4 of Jones and Kiniry (1986)</td>
</tr>
<tr>
<td>Light extinction coefficient ($k$). The default value is for modern maize hybrids</td>
<td>0.55</td>
<td>Lizaso et al. (2003b), Maddonni et al. (2001) and this study</td>
</tr>
<tr>
<td>Fraction of leaf mass that can be translocated to grain per day if leaf mass remains above minimum</td>
<td>0.005 per day</td>
<td>Jones and Kiniry (1986)</td>
</tr>
<tr>
<td>Minimum fraction of leaf mass below which no translocation of carbohydrate from leaf to grain is allowed</td>
<td>0.85</td>
<td>Jones and Kiniry (1986)</td>
</tr>
<tr>
<td>Growth respiration coefficient of leaf</td>
<td>0.47 g CH$_2$O g$^{-1}$ dry matter</td>
<td>Kropff and van Laar (1993)</td>
</tr>
<tr>
<td>Growth respiration coefficient of stem</td>
<td>0.52 g CH$_2$O g$^{-1}$ dry matter</td>
<td>Kropff and van Laar (1993)</td>
</tr>
<tr>
<td>Growth respiration coefficient of root</td>
<td>0.45 g CH$_2$O g$^{-1}$ dry matter</td>
<td>Kropff and van Laar (1993)</td>
</tr>
<tr>
<td>Growth respiration coefficient of grain</td>
<td>0.49 g CH$_2$O g$^{-1}$ dry matter</td>
<td>Kropff and van Laar (1993)</td>
</tr>
<tr>
<td>Maintenance respiration coefficient for leaf</td>
<td>0.01 g CH$_2$O g$^{-1}$ dry matter per day</td>
<td>Through calibration in this study</td>
</tr>
<tr>
<td>Maintenance respiration coefficient for stem</td>
<td>0.006 g CH$_2$O g$^{-1}$ dry matter per day</td>
<td>Through calibration in this study</td>
</tr>
<tr>
<td>Maintenance respiration coefficient for root</td>
<td>0.005 g CH$_2$O g$^{-1}$ dry matter per day</td>
<td>Through calibration in this study</td>
</tr>
<tr>
<td>Maintenance respiration coefficient for grain</td>
<td>0.005 g CH$_2$O g$^{-1}$ dry matter per day</td>
<td>Through calibration in this study</td>
</tr>
<tr>
<td>Efficiency of carbohydrate translocation</td>
<td>0.26</td>
<td>Kiniry et al. (1992)</td>
</tr>
<tr>
<td>Daily root death rate in fraction</td>
<td>0.005</td>
<td>Jones and Kiniry (1986)</td>
</tr>
<tr>
<td>Stay-green coefficient in Eq. (10)</td>
<td>4</td>
<td>This study</td>
</tr>
<tr>
<td>Fraction of dead leaf at maturity in maximum LAI achieved at silking</td>
<td>0.7</td>
<td>This study</td>
</tr>
<tr>
<td>Upper effective temperature for GDD accumulation</td>
<td>34 °C</td>
<td>Jones and Kiniry (1986)</td>
</tr>
<tr>
<td>Assimilation rate at plateau ($A_{\text{max}}$)</td>
<td>7.0 g CO$_2$ m$^{-2}$ leaf h$^{-1}$</td>
<td>Kropff and van Laar (1993)</td>
</tr>
<tr>
<td>Minimum temperature for assimilation</td>
<td>8 °C</td>
<td>Kropff and van Laar (1993)</td>
</tr>
</tbody>
</table>
### Appendix A (Continued)

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Default value</th>
<th>Reference</th>
</tr>
</thead>
<tbody>
<tr>
<td>Starting temperature for maximum assimilation</td>
<td>18 °C</td>
<td>Kropff and van Laar (1993)</td>
</tr>
<tr>
<td>Ending temperature for maximum assimilation</td>
<td>30 °C</td>
<td>Kropff and van Laar (1993)</td>
</tr>
<tr>
<td>Initial light use efficiency</td>
<td>12.5 g CO₂ MJ⁻¹ PAR</td>
<td>Kropff and van Laar (1993)</td>
</tr>
<tr>
<td>Upper effective temperature for maintenance respiration</td>
<td>30 °C</td>
<td>Kropff and van Laar (1993)</td>
</tr>
<tr>
<td>LAI above which stress due to light competition occurs</td>
<td>4</td>
<td>Jones and Kiniry (1986)</td>
</tr>
<tr>
<td>Biomass partitioning coefficient for root at emergence</td>
<td>0.35</td>
<td>Kropff and van Laar (1993)</td>
</tr>
<tr>
<td>Development stage (scale from 0 to 2 with silking as 1) when root growth stops</td>
<td>1.15</td>
<td>Kropff and van Laar (1993)</td>
</tr>
<tr>
<td>Offset for calculating $\text{GDD}<em>{\text{silking}}$ from $\text{GDD}</em>{\text{total}}$</td>
<td>−50</td>
<td>This study</td>
</tr>
</tbody>
</table>
References


Soil Survey Staff, 1999. Soil taxonomy: a basic system of soil classification for making and interpreting soil surveys. USDA-NRCS, Washington, DC.


