

## Limits to maize productivity in Western Corn-Belt: A simulation analysis for fully irrigated and rainfed conditions

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### ABSTRACT

Unlike the Central and Eastern U.S. Corn-Belt where maize is grown almost entirely under rainfed conditions, maize in the Western Corn-Belt is produced under both irrigated (3.2 million ha) and rainfed (4.1 million ha) conditions. Simulation modeling, regression, and boundary-function analysis were used to assess constraints to maize productivity in the Western Corn-Belt. Aboveground biomass, grain yield, and water balance were simulated for fully irrigated and rainfed crops, using 20-year weather records from 18 locations in combination with actual soil, planting date, plant population, and hybrid-maturity data. Mean values of meteorological variables were estimated for three growth periods (pre- and post-silking, and the entire growing season) and used to identify major geospatial gradients. Linear and stepwise multiple regressions were performed to evaluate variation of potential productivity in relation to meteorological factors. Boundary functions for water productivity and water-use efficiency were derived and compared against observed data reported in the literature. Geospatial gradients of seasonal radiation, temperature, rainfall, and evaporative demand along the Western Corn-Belt were identified. Yield potential with irrigation did not exhibit any geospatial pattern, depending instead on the specific radiation/temperature regime at each location and its interaction with crop phenology. A linear and parabolic response to post-silking cumulative solar radiation and mean temperature, respectively, explained variations on yield potential. Water-limited productivity followed the longitudinal gradient in seasonal rainfall and evaporative demand. Rainfed crops grown in the Western Corn-Belt are frequently subjected to episodes of transient and unavoidable water stress, especially around and after silking. Soil water at sowing ameliorates, but does not eliminate water stress episodes. Boundary functions for water productivity had slopes of 46 and 28 kg ha<sup>-1</sup> mm<sup>-1</sup>, for aboveground biomass and grain yield, respectively. At high seasonal water supply, productivity was weakly correlated with water supply because many crops did not fully utilize seasonally available water due to percolation below the root zone or water left in the ground at physiological maturity. Fitted boundary functions for water-use efficiency had slopes ( $\approx$ seasonal transpiration-efficiency) of 54 and 37 kg ha<sup>-1</sup> mm<sup>-1</sup> for aboveground biomass and grain yield, respectively, and an  $x$ -intercept around 25–75 mm ( $\approx$ seasonal soil evaporation). Data collected from experiments conducted in low-rainfall environments indicated that the boundary functions for water-use efficiency, derived from this study, are broadly applicable.

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### 1. Introduction

Yield potential is defined as the yield of a crop cultivar when grown in an environment to which it is adapted, with nutrient and water non-limiting and pests and diseases effectively controlled (Evans, 1993). Hence, yield potential for a given genotype is determined by the particular combination of solar radiation, temperature and plant population at a specific location (van Ittersum and Rabbinge, 1997). Yield potential can be diminished as

a consequence of insufficient water supply to meet crop water demand. Thus, water-limited yield is determined by the genotype, solar radiation, temperature, plant population and the degree of water limitation (Loomis and Connor, 1992). Insufficient water supply can result from sub-optimal seasonal water supply (stored soil water plus growing-season rainfall) in rainfed systems or sub-optimal irrigation in irrigated systems. Accurate quantification of yield potential and water-limited limited yield is essential to estimate the magnitude of the exploitable gap between actual (*i.e.*, those achieved by farmers) and attainable yields, to predict global change scenarios, and to help formulate policies to ensure local and global food security (Cassman et al., 2003). The lack of data from experiments in which yield-limiting factors have been effectively

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controlled makes it difficult to obtain reliable quantifications of yield-potential and water-limited yield based on actual measurements (Duvick and Cassman, 1999). When such data are lacking, simulation models can provide reasonable estimates of yield potential and water-limited yields when soil and historical daily weather data are available, including solar radiation, daily temperature, and rainfall (e.g., Amir and Sinclair, 1991a,b; Yang et al., 2004).

Although maize production is expected to increase substantially to meet the rapidly increasing demand for food, livestock feed, and biofuel at a global scale (Cassman et al., 2003; Cassman and Liska, 2007), there has been little increase in maize yield potential in the last 30 years (Duvick and Cassman, 1999; Tollenaar and Lee, 2002). Studies attempting to understand maize yield potential and its variation in relation to environmental factors have highlighted the crucial role of solar radiation and temperature (Muchow, 1989; Cirilo and Andrade, 1994; Otegui et al., 1995, 1996). A few studies have attempted to quantify yield potential and its variation at a regional scale using observed data (Duncan et al., 1973; Andrade et al., 1996) and simulation modeling (Hodges et al., 1987; Muchow et al., 1990; Wilson et al., 1995; Löffler et al., 2005). In all of these studies, maize yields were evaluated against mean meteorological variables for the entire growing season rather than specific growth phases that are most sensitive to environmental limitations (Otegui and Bonhomme, 1998). Likewise, it was not clear if the practices used at all locations were optimal for maximum attainable yield. As a result, measured or simulated yields appear to be well below maize yield potential. Finally, simulation models such as CERES-Maize (Jones and Kiniry, 1986) and the Muchow–Sinclair–Bennett model (Muchow et al., 1990) do not account explicitly for direct effects of temperature on gross carbon assimilation and respiration, which may have a significant impact on yield estimates in cool or warm environments (e.g., Edmeades and Bolaños, 2001).

Water resources for agriculture are heavily exploited and there is increasing competition for limited water supplies in most countries with extensive irrigated agriculture (Rosegrant et al., 2002). Therefore, quantifying the maximum yield per unit of available water supply, hereafter called the water-limited yield, is essential for identifying water management practices and policies to optimize water-use efficiency (Wallace, 2000). Boundary functions provide a robust framework to analyze water-limited productivity (e.g., French and Schultz, 1984; Passioura, 2006; Sadras and Angus, 2006). Yield is plotted against either: (i) water supply (stored soil water at sowing plus rainfall), or (ii) crop evapotranspiration ( $ET_c$ ), on a seasonal basis, and a linear function is fitted to those data that delimit the upper frontier for yield. The first approach, namely water productivity (WP), provides a benchmark to help farmers set target yields and identify other yield reducing-factors, such as nutrients, pests, and diseases (Passioura, 2006). The second approach based on  $ET_c$ , namely water-use efficiency (WUE), provides a physiological frontier for water-limited productivity in which the slope represents the seasonal transpiration-efficiency ( $TE_s$ ) and the  $x$ -intercept gives a rough estimate of seasonal soil evaporation (Sinclair et al., 1984). Despite the large number of reported yield/water supply relationships reported for maize, we were not able to find any explicit attempt to define maximum boundary functions for water productivity or water-use efficiency.

To fill this knowledge gap about maize productivity and its variability, we used a crop simulation model (Yang et al., 2004), regression and boundary function analysis to assess limits to maize aboveground biomass and grain yield in the Western Corn-Belt. The primary objectives of this work were to: (i) identify geospatial patterns of radiation, temperature, rainfall, reference evapotranspiration, and water-stress; (ii) explain geospatial variations in

potential and water-limited productivity in relation to these climate variables; and (iii) determine boundary functions for water productivity and water-use efficiency.

## 2. Materials and methods

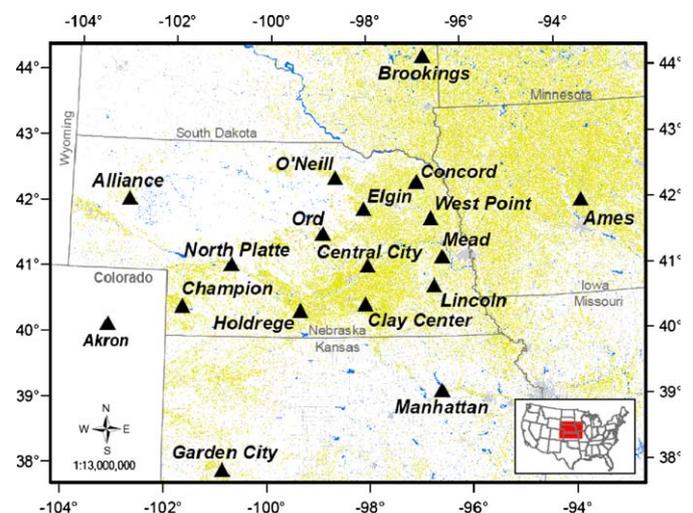
### 2.1. The Western Corn-Belt

The Western U.S. Corn-Belt (37–45°N; 92–105°W) includes about 7.3 million ha cultivated with maize, mostly located in Kansas, Nebraska, and South Dakota states (Fig. 1) (USDA-NASS, 2003–2007). Irrigated maize represents 43% of the total maize area (70% of the total irrigated cropland in the region) and accounts for 58% of the total annual maize production of 60 million Mg in the Western Corn-Belt. Average county-level yields range from 2.4 to 8.1 Mg ha<sup>-1</sup> under rainfed conditions, and from 8 to 11.2 Mg ha<sup>-1</sup> with irrigation. These values are well below the highest reported yields for rainfed (9–16 Mg ha<sup>-1</sup>) and irrigated maize (15–21 Mg ha<sup>-1</sup>) in the region (Duvick and Cassman, 1999).

Soil and climate in the region are described by Smika (1992). The landscape is undulate. Predominant agricultural soils are Haplustolls and Argiustolls with medium-to-high water holding capacity. Elevation increases by 118 m per longitude degree, from east to west (range: 309 m in Ames, IA to 1384 m in Akron, CO). The climate is continental and temperate, and the frost-free period decreases from the southeast to the northwest along the altitudinal gradient. Annual rainfall decreases from east to west, and its distribution follows a monsoonal pattern: 70–80% of the precipitation is concentrated in the spring and summer seasons. Evaporative demand exceeds rainfall during the summer growing-season such that most rainfed crops depend on stored soil moisture that accumulates from snow melt and spring rains (Loomis and Connor, 1992).

### 2.2. Model evaluation

Hybrid-Maize (Yang et al., 2004, 2006) is a process-oriented model that simulates maize development and growth on a daily time step under growth conditions without limitations from nutrient deficiencies or toxicities, or from insect pests, diseases, or weeds. It features temperature-driven maize development, vertical canopy integration of photosynthesis, organ-specific growth respiration, and temperature-sensitive maintenance respiration.



**Fig. 1.** Map of the Western U.S. Corn-Belt. States are named and their boundaries shown. Triangles indicate sites of meteorological stations used in this study. Inset shows location of area within U.S. Maize (yellow), water (blue), and urban (grey) areas are shown, except for Wyoming and Colorado (data not available).

**Table 1**  
Dataset for Hybrid-Maize validation for rainfed and fully irrigated crops.

Location	Seasons	<i>n</i>	Yield (Mg ha <sup>-1</sup> ) <sup>a</sup>	Sources
<i>Fully irrigated crops</i>				
Bellwood, NE <sup>b</sup>	2003	1	16.8	Dobermann et al. (unpublished data)
Brunswick, NE	2003	1	17.4	Dobermann et al. (unpublished data)
Cairo, NE	2003	1	17.3	Dobermann et al. (unpublished data)
Clay Center, NE	2002, 2005, 2006	3	14.5–16.2	Dobermann et al. (unpublished data), Yang et al. (unpublished data)
Edgar, NE	2007	1	13.6	Yang et al. (unpublished data)
Geneva, NE	2007	1	13.3	Yang et al. (unpublished data)
Hordville, NE	2007	1	12.8	Yang et al. (unpublished data)
Lincoln, NE	1999–2003	11	14.8–17.9	Yang et al. (2004), Dobermann et al. (unpublished data), Dobermann and Walters (2004)
Mead, NE	2002–2007	3	13–15.5	Dobermann et al. (unpublished data), Yang et al. (unpublished data)
North Platte, NE	2003–2006	2	13.3–14.2	Yang et al. (unpublished data)
Paxton, NE	2003	1	16.2	Dobermann et al. (unpublished data)
Scandia, KS	2003	2	14–15.7	Dobermann and Walters (2004)
York, NE	2007	1	14.9	Yang et al. (unpublished data)
West Point, NE	2007	1	15	Yang et al. (unpublished data)
<i>Rainfed crops</i>				
Champaign, IL	2003	1	16.4	Dobermann and Walters (2004)
Clay Center, NE	2005–2006	2	3.9–7.7	Yang et al. (unpublished data)
Manchester, IA	2002	1	16	Yang et al. (2004)
Mead, NE	2001, 2003, 2005	3	7.7–9.9	Walters et al. (unpublished data)
North Platte, NE	1992–1995, 2005, 2006	6	0.6–13	Payero et al., 2006, Yang et al. (unpublished data)

<sup>a</sup> Measured yields at standard moisture, 0.155 kg H<sub>2</sub>O kg<sup>-1</sup> grain.

<sup>b</sup> Locations and corresponding USA state (IL: Illinois; IA: Iowa; KS: Kansas; NE: Nebraska).

Simulation of photosynthesis, growth respiration and maintenance respiration may make the Hybrid-Maize model more responsive to changes in environmental conditions than models such as CERES-Maize or the Muchow-Sinclair-Bennett model, which utilize radiation-use efficiency (RUE) to integrate the processes of assimilation and respiration. The results presented here extend the original model validation reported by Yang et al. (2004).

Maize yields were obtained from field studies conducted over 43 site-years that including rainfed (*n* = 13) and fully irrigated (*n* = 30) field studies (Table 1). The database did not include fields with obvious limitations due to nutrient deficiencies, diseases, insects, weeds, hail or waterlogging. Simulated grain yields were compared against observed values and root mean square error (RMSE) was calculated. For rainfed crops, available soil water at sowing (ASW<sub>s</sub>) was estimated based on rainfall during the period from October to the planting date at each site, soil water holding capacity, and simulated ASW left in the ground by the previous maize crop (data not shown). Temperature and radiation data were obtained from the nearest meteorological station, which, on average, was located ≈14 km away from each field (range: 0–40 km). Rainfall was recorded at the field study site in 75% of the site-years or at the nearest meteorological station. Simulations were based on the actual soil texture, planting date, plant population, and hybrid used at each site. Grain yields for this model evaluation, and for all other simulations in this paper, are reported at a standard moisture content of 0.155 kg H<sub>2</sub>O kg<sup>-1</sup> grain.

### 2.3. Simulated yield and water balance

Rainfed and irrigated yield were simulated at 18 sites across the Western Corn-Belt (Fig. 1). Grain yield, aboveground biomass on an oven-dry basis, and water balance components [soil evaporation, crop evapotranspiration (ET<sub>c</sub>), percolation below root zone, and residual ASW at maturity] were simulated using long-term (20-year) weather records. Simulations utilized the actual soil type, average sowing date, and the recommended hybrid-maturity for each site (Table 2). Average sowing date was the date when 50% of the total maize area was planted according to 2004–2006 county-level report on planting progression obtained from the Risk

Management Agency-USDA (Rebecca Davis, personal communication). The predominant soil series suitable for maize production was identified in an area of 710 km<sup>2</sup> around each meteorological station using STATSGO (USDA, 1994) and SSURGO (USDA, 1995) databases, and the soil texture of that soil series, derived from the official soil series descriptions (USDA-NRCS), was specified in the rainfed simulations because soil water retention and release characteristics are based on soil texture in Hybrid-Maize. None of these soils have physical impediments to root growth and so root depth was set at 1.5 m, based on soil water extraction patterns reported by Payero et al. (2006).

The recommended plant population and hybrid-maturity for each location were provided by agronomists from a major seed company. A fixed plant population (80,000 plants ha<sup>-1</sup>) was set for irrigated crops because recommended population did not vary across locations with irrigation. In contrast, recommended plant populations varied from 32,000 to 78,000 plants ha<sup>-1</sup> along the west–east gradient of increasing rainfall (Table 2; Appendix A, Fig. A1). Site-years in which minimum temperature fell below freezing during grain-filling were not allowed to exceed 25% of the 20-year simulation period (Table 2). Simulations ended at physiological maturity for the recommended hybrid at each site. Two ASW<sub>s</sub> scenarios were simulated for rainfed crops: fully recharged profile (FRP, whole profile at 100% ASW) and partially recharged profile (PRP; upper 0.3 m at 100% ASW, rest of the profile at 25% ASW). The scenarios are representative of the expected range in ASW<sub>s</sub>, based on: (i) 3-year ASW data at eight locations between 97 and 104°W along the east–west rainfall gradient (data provided by the High-Plains Regional Climate Center), (ii) 20-year water balance computations during the fallow's period, and (iii) our expert opinion.

### 2.4. Geospatial patterns of meteorological variables and productivity

For each site-year simulation, mean values for the following meteorological variables were estimated: daily and cumulative incident solar radiation, daily maximum (*T*<sub>max</sub>), mean (*T*<sub>mean</sub>) and minimum temperature (*T*<sub>min</sub>), daily relative humidity, cumulative rainfall, and cumulative ET<sub>O</sub> (estimated using Penman's equation). Means were calculated for the entire crop cycle (*i.e.*, from sowing to

**Table 2**

Dataset for modeling analysis of fully irrigated and rainfed maize yield at different locations in Western U.S. Corn-Belt using historical climate data (1986–2005).

Location	Dominant soil series	% of total agricultural land <sup>a</sup>	Planting date <sup>b</sup>	Hybrid-maturity <sup>c</sup>	Plant population <sup>d</sup>	Frost incidence <sup>e</sup>
Akron, CO <sup>f</sup>	Platner	35	130	1400	32,000	15
Alliance, NE	Creighton	57	128	1220	§	20
Ames, IA	Clarion	30	115	1472	78,000	10
Brookings, SD	Kranzburg-Brookings	15	124	1172	74,000	20
Central City, NE	Holder	20	119	1524	63,000	25
Champion, NE	Goshen	10	125	1417	35,000	25
Clay Center, NE	Hastings	43	113	1510	54,000	20
Concord, NE	Moody	33	123	1382	67,000	20
Elgin, NE	Moody	22	121	1438	54,000	15
Garden City, KS	Richfield	40	121	1524	44,000	0
Holdrege, NE	Holdrege	91	117	1510	49,000	10
Lincoln, NE	Aksarben	37	113	1524	69,000	10
Manhattan, KS	Reading	12	106	1510	59,000	0
Mead, NE	Yutan	22	120	1524	64,000	5
North Platte, NE	Holdrege	18	124	1405	44,000	20
O'Neill, NE	Jansen	53	123	1340	54,000	25
Ord, NE	Holdrege	20	125	1450	58,000	20
West Point, NE	Moody	40	120	1510	64,000	25

<sup>a</sup> Percentage of the dominant soil series land suitable for maize production with respect to the total agricultural land in the area (710 km<sup>2</sup>) surrounding each location. Data derived from STATSGO (USDA, 1994) and SSURGO (USDA, 1995) databases.

<sup>b</sup> Day of year.

<sup>c</sup> Sowing-to-physiological maturity growing degree days ( $T_b = 10$  °C).

<sup>d</sup> Plant population for rainfed crops (plants ha<sup>-1</sup>). Plant population for fully irrigated crops was set at 80,000 plants ha<sup>-1</sup> at all locations.

<sup>e</sup> Percentage of years with early frost during grain-filling.

<sup>f</sup> Location and corresponding USA state (CO: Colorado; IL: Illinois; IA: Iowa; KS: Kansas; NE: Nebraska; SD: South Dakota).

§ No significant rainfed maize production at this location.

physiological maturity), the pre-silking (*i.e.*, from sowing to silking), and post-silking (*i.e.*, from silking to physiological maturity) phases. 20-Year mean values at each location were then plotted against latitude and longitude to identify major geospatial gradients. Linear or second-order polynomial functions were fitted. A similar analysis was performed to identify geospatial patterns in potential and rainfed aboveground biomass and grain yield.

### 2.5. Growing-season rainfall, evaporative demand, and water stress patterns

Hybrid-Maize was used to evaluate seasonal rainfall, crop water use, and water stress patterns of rainfed maize over 20 years of weather data at Akron, CO and Mead, NE, which are representative of the longitudinal gradients of rainfall and ET<sub>O</sub> in the Western Corn-Belt (Fig. 1). Model inputs for each site are shown in Table 2. The crop growth period, from sowing to physiological maturity, was divided into 20-day intervals. For each interval, mean and tercile values were calculated for cumulative rainfall, cumulative maximum ET<sub>C</sub> (*i.e.*, the ET<sub>C</sub> a crop would have when grown under non-water limiting conditions), and average water-stress index (WSI). Hybrid-Maize simulates maximum ET<sub>C</sub> as a function of the evaporative demand and leaf area. WSI is the ratio between actual transpiration and potential transpiration (range: 0 [no stress] to 1 [maximum stress]; see Yang et al., 2006). WSI patterns were simulated for the two ASW<sub>S</sub> scenarios (FRP and PRP initial soil water).

### 2.6. Explanation of geospatial variation in aboveground biomass and grain yield

Pearson's correlations between site-year means of meteorological variables (Section 2.4) and aboveground biomass or grain yield were evaluated for both fully irrigated and rainfed conditions for the entire growth cycle and the pre- and post-silking phases. Stepwise multiple-regression analysis (Kleinbaum et al., 1998) was performed to explain the simulated variability in potential aboveground biomass and grain yield (dependent variables) on meteorological variables (independent variables). The objective

was to determine whether using mean meteorological values for both the vegetative and reproductive phases as independent variables, instead of means for the entire crop growth cycle, can explain significantly more of the simulated variation in potential aboveground biomass and grain yield. Because there was a high degree of co-linearity between  $T_{\text{mean}}$  and  $T_{\text{max}}$ , and between  $T_{\text{mean}}$  and  $T_{\text{min}}$  (data not shown), stepwise regressions used either  $T_{\text{mean}}$  or both  $T_{\text{max}}$  and  $T_{\text{min}}$ . Cumulative solar radiation was chosen as an independent variable instead of daily radiation because: (i) the former integrates both daily radiation and differences in hybrid maturity among locations (Table 2), and (ii) daily radiation and  $T_{\text{max}}$  were highly correlated ( $r \approx 0.7$ ). Separate stepwise regression analyses ( $p > 0.05$  for variable rejection) were performed with different sets of independent variables for (i) the entire crop cycle and (ii) both pre- and post-silking phases. Additional quadratic terms for temperature were added into the model to account for curvilinear responses. The predictive value of each variable was quantified in terms of its relative contribution to the regression sum of squares (%SSR), the latter computed as the difference between the total sum of squares and the residual sum of squares.

### 2.7. Boundary-function analysis

The quantile regression method of Cade and Noon (2003) was used to derive maximum boundary functions for the relationships between simulated aboveground biomass or grain yield and seasonal water supply (ASW<sub>S</sub> + growing-season rainfall + irrigation) or ET<sub>C</sub>. Fully irrigated ( $n = 295$ ) and rainfed ( $n = 564$ ) frost-free site-years were pooled across ASW<sub>S</sub> scenarios. To derive the boundary function, seasonal water supply and ET<sub>C</sub> values for the 200–800 mm and 200–600 mm intervals were split into 10 classes; these ranges represent the water supply and ET<sub>C</sub> levels in which grain yield is responsive to changes in water status. The 95th percentile of class biomass or yield was regressed against the water-availability or ET<sub>C</sub> mid-point of each class. Fitted functions represented the maximum boundary line for WP and WUE, respectively.

Boundary functions derived for WUE were compared against observed data for aboveground biomass ( $n = 263$ ) or grain yield

( $n = 556$ ) versus  $ET_C$ , obtained from the literature for maize grown in low-rainfall environments (Appendix B). In these studies maize relied on stored ASW, seasonal rainfall, and in some cases, irrigation. Reported  $ET_C$  was generally calculated as growing-season rainfall and irrigation plus the change in ASW of the root zone between sowing and harvest.

### 3. Results

#### 3.1. Model validation

The Hybrid-Maize model simulated yields reasonably well in the Western Corn-Belt as 100% and 70% of predicted grain yield were within  $\pm 15\%$  of measured values for fully irrigated and rainfed crops, respectively, across a broad range of growth conditions and yield potential (Fig. 2). Grain yield was overestimated at very low observed yields ( $< 2 \text{ Mg ha}^{-1}$ ) and for two cases in the moderate yield range between 6 and  $9 \text{ Mg ha}^{-1}$ . Examination of climate data during the growing season for these four site-years identified severe water deficits during the 3 weeks immediately before and shortly after silking (data not shown). Although maize yields are highly sensitive to water deficits during the period immediately before and after silking through effects on pollination and kernel setting (Hall et al., 1982; Westgate and Boyer, 1986), Hybrid-Maize does not explicitly simulate the direct effects of water deficits on kernel number. It is therefore likely the discrepancies between observed and simulated values in these four site-years were due to lack of adequate sensitivity in the Hybrid-Maize model to severe moisture deficits during the silking window.

#### 3.2. Geospatial gradients of climate and crop water demand

Geospatial trends in meteorological variables differed for cumulative solar radiation and  $T_{\text{mean}}$  depending on the crop growth time period and direction. For example, while  $T_{\text{mean}}$  was relatively constant across the longitudinal gradient of the Western Corn-Belt, cumulative solar radiation increased from  $2560 \text{ MJ m}^{-2}$  in the east to  $3203 \text{ MJ m}^{-2}$  in the west, and this gradient was most pronounced in the pre-silking growth period (Fig. 3(a)–(c)). In contrast, cumulative solar radiation was relatively constant across the latitudinal gradient while  $T_{\text{mean}}$  for the entire growing season increased from  $18.5^\circ\text{C}$  in the north to  $22.4^\circ\text{C}$  in the south, and this increase was most pronounced in the post-silking phase

(Fig. 3(d)–(f)).  $T_{\text{max}}$  increased from north–south in both the pre- and post-silking phases ( $p < 0.0001$ ,  $r^2 = 0.61$  and  $0.76$ , respectively), while no latitudinal variation in  $T_{\text{min}}$  was detected (data not shown). The length of the free-frost season also increased from north–south (data not shown). Although  $T_{\text{mean}}$  was similar across longitude, the mean thermal amplitude (i.e., the difference between mean daily minimum and maximum temperature) increases dramatically in the east–west direction ( $p < 0.0001$ ,  $r^2 = 0.92$ ).

Longitudinal gradients were found for seasonal rainfall and  $ET_O$  (Fig. 3(g)–(i)), whereas both variables were relatively constant across the north–south direction (data not shown). From east to west, rainfall decreases (range: 210–555 mm) while  $ET_O$  increases (range: 485–790 mm).  $ET_O$  gradient was related to the increase in solar radiation (Fig. 3(a)) and decrease in relative humidity ( $p < 0.0001$ ,  $r^2 = 0.89$ ) in the east–west direction. At all locations, the variability in rainfall during the entire growing season was much greater across years than  $ET_O$  (coefficient of variation [CV] = 0.40 for rainfall versus 0.12 for  $ET_O$ ), especially during the post-silking phase (Fig. 3(g)–(i)). Trends in the recommended rainfed plant population closely follow the east–west rainfall and  $ET_O$  gradients, reflecting management adaptation to reduced water supply (Appendix A, Fig. A1).

#### 3.3. Seasonal patterns of rainfall, maximum $ET_C$ and water-stress index

The mean and standard error (20-year) for rainfall during the entire growing-season were  $286 \pm 33$  and  $398 \pm 26$  mm at Akron CO and Mead NE, respectively. At both locations, maximum  $ET_C$  ( $820 \pm 13$  at Akron and  $607 \pm 14$  mm at Mead, respectively) exceeds growing-season rainfall by a large margin. While rainfall exceeds  $ET_C$  in May, which is the first month after planting, it remains well below crop water demand throughout the remainder of the growing season, especially at Akron (Fig. 4(a) and (b)), which represents the western edge of the longitudinal gradient in this study (Fig. 1). Maximum crop water demand peaks in late June and early July, about 2 months after planting and remains relatively high throughout the remainder of the growing season (Fig. 4(a) and (b)). Annual variation in rainfall was large at both locations for each 20-day period throughout the growing season (CV = 0.85 and 0.75 at Akron and Mead, respectively) compared to the much smaller annual variation in  $ET_C$  (CV = 0.21 and 0.25, respectively). Simulated average WSI indicates that maize grown in the Western Corn-Belt will experience transient water stress events from pre-silking phase about 60 days after sowing until physiological maturity in most years with the magnitude and probability of water stress increasing as the season progresses (Fig. 4(c) and (d)). Average stress severity was greater and more likely at Akron than in Mead, in agreement with the east–west gradient in rainfall and  $ET_O$  (Fig. 3(g)–(i)). At both locations, greater stored soil moisture at sowing reduced the magnitude of water stress from pre-silking to maturity although the magnitude of reduction was relatively small (Fig. 4(c) and (d)).

#### 3.4. Geospatial patterns in potential and water-limited yields

Potential grain yield was not well correlated with longitudinal or latitudinal trends ( $p > 0.10$ ), although highest yields were mostly achieved at intermediate latitudes ( $40\text{--}42.5^\circ\text{N}$ , data not shown). In contrast, there was a strong latitudinal gradient in potential aboveground biomass ( $p < 0.01$ ,  $r = -0.81$ ), mostly due to warmer daytime temperatures during the entire crop cycle. In rainfed crops, there was a sharp longitudinal gradient of aboveground biomass ( $p < 0.0005$ ,  $r = 0.76$ ) and grain yield ( $p < 0.0001$ ,  $r = 0.81$ ), associated with seasonal rainfall and  $ET_O$  gradients (Fig. 3(g)–(i), Table 3). Mean potential grain yield ranged from 11.4

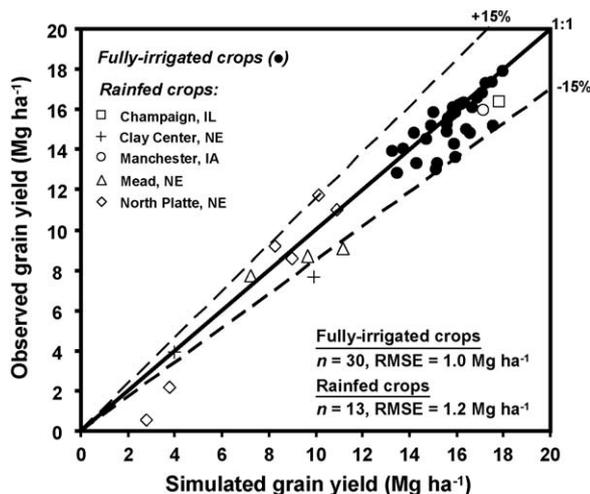
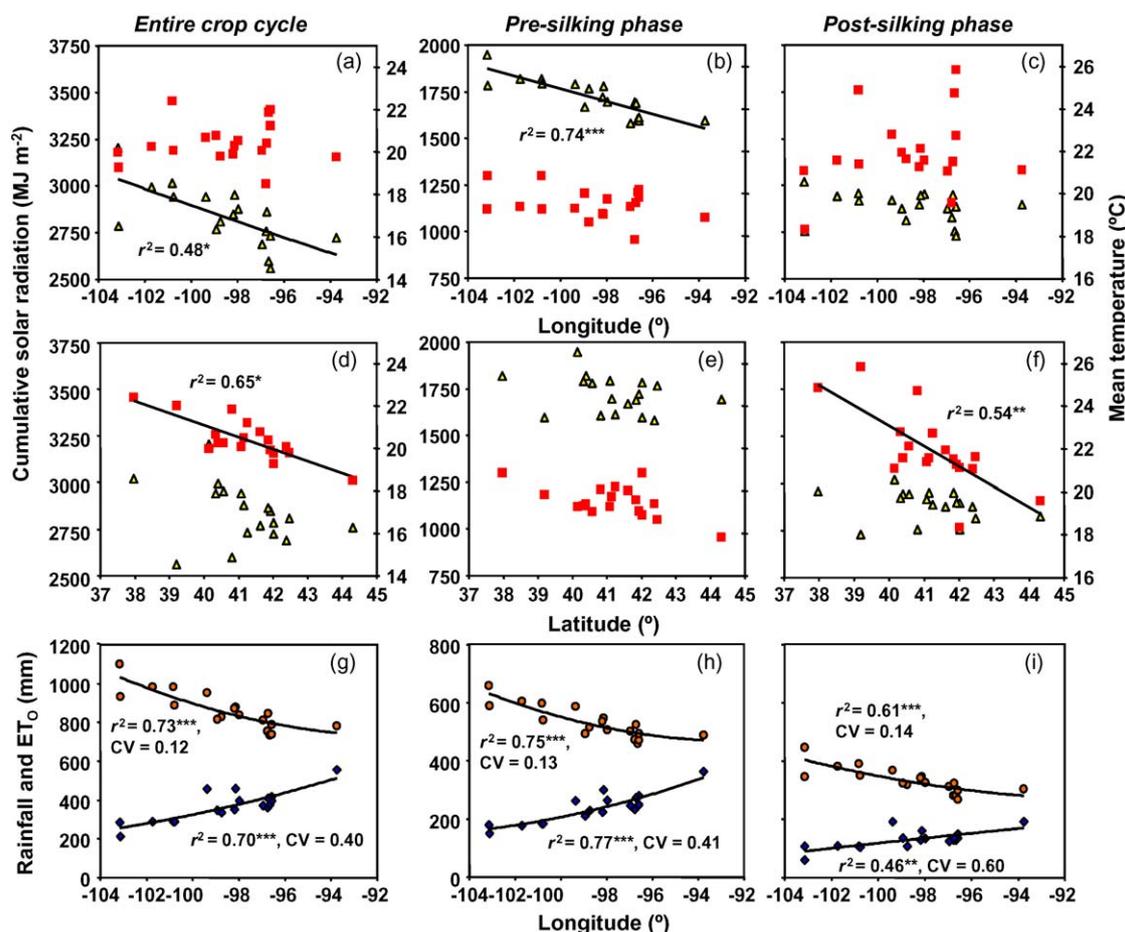


Fig. 2. Observed vs. simulated yields for a test set of fully irrigated and rainfed maize crops grown in the U.S. Corn-Belt (see Table 1 for more details). Diagonal solid line: 1:1 ratio; dotted lines:  $\pm 15\%$  deviation from 1:1 line. Separate root mean square errors (RMSE) for fully irrigated and rainfed crops are shown.



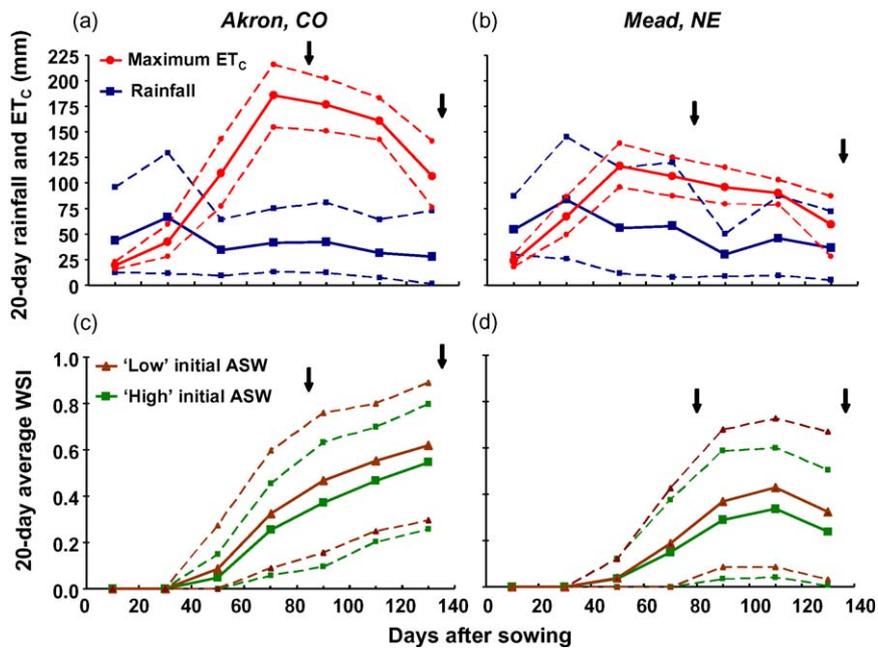
**Fig. 3.** Longitudinal and latitudinal gradients of selected meteorological factors during the entire crop cycle (left panels), the pre-silking phase (central panels), and the post-silking phase (right panels). (a–f) Cumulative solar radiation (yellow triangles) and mean temperature (red squares); (g–i) cumulative rainfall (blue diamonds) and reference evapotranspiration ( $ET_0$ , orange circles). No latitudinal gradients of cumulative rainfall and  $ET_0$  were found, thus, these plots are not shown. Each point is the 20-year average for a given location. Crops affected by early frost were not accounted. SE ranges, across locations, between 34–82, 15–52, and 21–38  $MJ m^{-2}$  for cumulative solar radiation and between 0.2–0.3, 0.2–0.4, and 0.3–0.6  $^{\circ}C$  for mean temperature, for the entire crop cycle, pre-, and post-silking phases, respectively. Average inter-annual coefficients of variation (CV) for cumulative rainfall and  $ET_0$  are shown. Asterisks indicate correlation at  $p < 0.01$ ,  $^{**}p < 0.001$ , and  $^{***}p < 0.0001$ .

to 16.1  $Mg ha^{-1}$  across locations (mean: 14.4  $Mg ha^{-1}$ ) with a relatively small degree of annual variation ( $CV = 0.11$ ). Maximum simulated grain yields ( $\approx 17$ – $20 Mg ha^{-1}$ ) were similar to those reported by Duvick and Cassman (1999) for the same region. Rainfed yields were lower and considerably more variable: ‘high’ and ‘low’ ASW<sub>5</sub> scenarios averaged 8.8 and 7.6  $Mg ha^{-1}$ , respectively (associated  $CVs = 0.27$  and  $0.42$ ). Mean potential aboveground biomass yield averaged 26.1  $Mg ha^{-1}$  (range: 21.8–30.5  $Mg ha^{-1}$ ,  $CV = 0.07$ ), while mean rainfed aboveground biomass yield was 16.9 and 15.5 for the ‘high’ and ‘low’ ASW<sub>5</sub> scenarios, respectively (associated  $CVs = 0.20$  and  $0.27$ ). For both irrigated and rainfed conditions, the  $CVs$  for total aboveground biomass yield were smaller than for grain yield, and this difference was greatest in rainfed situations.

Highest aboveground biomass yields were found at locations where the length of the growing season and the recommended hybrid maturity resulted in large cumulative solar radiation values (Table 3, Fig. 5(a)), and where crops were subjected to warm temperatures during the vegetative phase (Table 3, Fig. 5(b)). Potential grain yield was most closely associated with post-silking cumulative solar radiation (Table 3, Fig. 5(c)). The significant parabolic relationship between simulated grain yield and post-silking  $T_{mean}$  suggests that both high ( $\approx > 25^{\circ}C$ ) and low ( $\approx < 20^{\circ}C$ ) mean daily temperatures during grain filling reduce grain yield potential (Fig. 5(d)). High post-silking  $T_{mean}$  reduced grain-filling duration ( $p < 0.001$ ,  $r^2 = 0.59$ ) and also increased maintenance

respiration as simulated by Hybrid-Maize (data not shown). On the other hand, low post-silking  $T_{mean}$  reduced both photosynthetic rates and kernel-growth rates (data not shown), and, in most cases, these effects were not offset by the increase in the grain-filling duration associated with low post-silking temperatures.

Stepwise regressions were performed separately for all site-years ( $n = 351$ ) and frost-free site-years ( $n = 295$ ) to test for inconsistencies in the final regression model but the variables selected and their coefficients were of similar magnitude and sign (data not shown). Therefore, we used the frost-free regression. Stepwise multiple-regression that included meteorological means for both vegetative and reproductive growth phases explained 86% and 70% of the variation on simulated potential aboveground biomass and grain yield, respectively (data not shown). Pre- and post-silking cumulative solar radiation and pre-silking maximum daily temperature had the greatest influence on potential aboveground biomass (%SSR = 35, 30, and 29%, respectively;  $p < 0.0001$ ). In contrast, potential grain yield was most closely related to post-silking cumulative radiation and mean daily temperature (%SSR = 89 and 6%, respectively;  $p < 0.001$ ). The negative effects of high temperatures on potential grain yield during grain filling were reflected by a significant quadratic term for post-silking  $T_{mean}$  ( $p < 0.005$ ). These results were consistent with the single-factor relationships quantified by Pearson’s correlation (Table 3) and regression (Fig. 5). Stepwise regressions using meteorological variable means for the entire growing season explained consider-



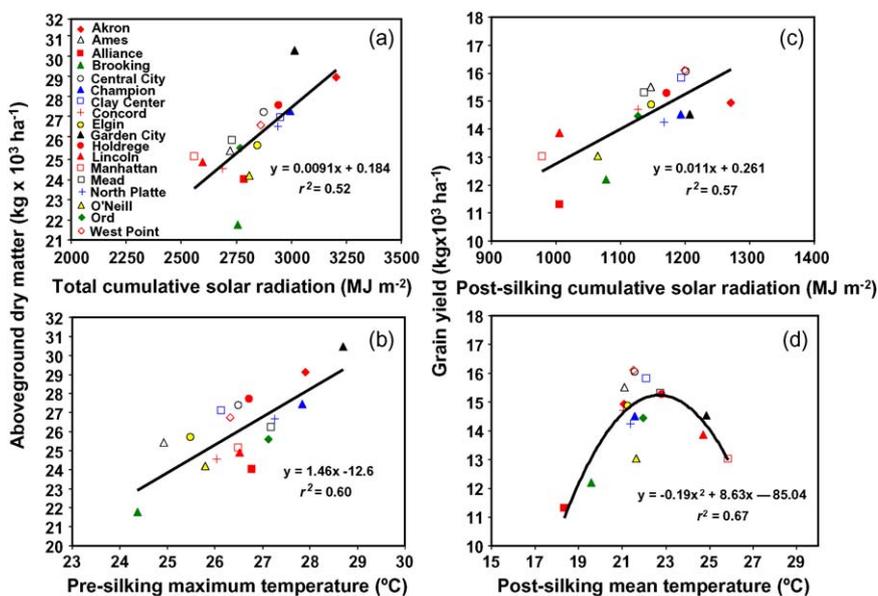
**Fig. 4.** Patterns of long-term (a and b) 20-day cumulative rainfall and crop evapotranspiration, under non-limiting water supply ( $ET_c$ ), and (c and d) 20-day average water-stress index (WSI) in simulated rainfed crops for two scenarios of available soil water (ASW) at sowing. Each point represents a 20-day interval. Solid thick lines: means; dashed thin lines: upper and lower terciles. Data come from selected stations in the area of interest, Akron, CO (right panels) and Mead, NE (left panels) (see Fig. 1). Sowing dates were 10 May and 30 April at Akron and Mead, respectively. Vertical arrows indicate average simulated dates of silking and physiological maturity (left and right arrows, in each figure, respectively).

ably less of the variation in simulated potential aboveground biomass and grain yield (adjusted  $r^2 = 0.70$  and  $0.48$ , respectively).

### 3.5. Boundary functions for water productivity and water-use efficiency

Rainfed maize yields were limited by the amount of water supply (Fig. 6(a) and (b)). Fitted boundary functions for WP had slopes of  $46.0 \pm 2.3$  and  $27.7 \pm 1.8 \text{ kg ha}^{-1} \text{ mm}^{-1}$  for aboveground biomass and grain yield, respectively (Fig. 6(a) and (b)). When seasonal water supply

was large, the relationship between yield and water supply weakened due to water losses by percolation below root zone and residual soil water at physiological maturity. Simulated percolation averaged  $105 \pm 6 \text{ mm}$  for fully irrigated crops and  $96 \pm 5$  and  $20 \pm 4 \text{ mm}$  for rainfed crops under 'high' and 'low' ASW<sub>s</sub>, respectively, and was associated with pre-silking rainfall ( $p < 0.001$ ,  $r^2 = 0.74, 0.78$ , and  $0.56$ ). Residual ASW at harvest averaged  $120 \pm 2 \text{ mm}$  for fully irrigated crops and  $88 \pm 3$  and  $52 \pm 4 \text{ mm}$  for rainfed crops under 'high' and 'low' ASW<sub>s</sub>, respectively, and was associated with post-silking rainfall ( $p < 0.001$ ,  $r^2 = 0.55, 0.63$ , and  $0.59$ ).



**Fig. 5.** Simulated potential aboveground dry matter yield as a function of total cumulative solar radiation and mean daily pre-silking maximum temperature (a and b), and simulated potential grain yield as a function of cumulative solar radiation and average mean temperature during the post-silking phase (c and d). Each point is the 20-year average at each simulated location (excluding those site-years in which a frost occurred during grain filling) in the Western U.S. Corn-Belt (see Fig. 1). All relationships were highly significant ( $p < 0.001$ ).

**Table 3**

Pearson's correlations coefficients between the simulated aboveground biomass or grain yield of fully irrigated ( $n = 295$ ) or rainfed ( $n = 564$ ) maize and means of environmental factors computed for the entire crop cycle (ECC), or the pre-silking (Pre-S) or post-silking (Post-S) phases. Site-years in which a frost occurred during grain-filling were not included.

Environmental factor	Fully irrigated crops		Rainfed crops <sup>a</sup>	
	Aboveground biomass	Grain yield	Aboveground biomass	Grain yield
<i>Daily radiation</i>				
Pre-S	0.53 <sup>***</sup>	-0.03	-0.38 <sup>***</sup>	-0.35 <sup>***</sup>
Post-S	0.56 <sup>***</sup>	-0.25 <sup>***</sup>	-0.40 <sup>***</sup>	-0.43 <sup>***</sup>
ECC	0.58 <sup>***</sup>	-0.15 <sup>**</sup>	-0.42 <sup>***</sup>	-0.42 <sup>***</sup>
<i>Cumulative radiation</i>				
Pre-S	0.51 <sup>***</sup>	0.22 <sup>***</sup>	-0.18 <sup>**</sup>	-0.16 <sup>**</sup>
Post-S	0.74 <sup>***</sup>	0.75 <sup>***</sup>	0.06	0.15 <sup>*</sup>
W	0.72 <sup>***</sup>	0.55 <sup>***</sup>	-0.08	0.02
<i>Mean temperature</i>				
Pre-S	0.23 <sup>***</sup>	-0.02	-0.21 <sup>***</sup>	-0.22 <sup>***</sup>
Post-S	0.07	-0.40 <sup>***</sup>	-0.27 <sup>***</sup>	-0.37 <sup>***</sup>
ECC	0.21 <sup>***</sup>	-0.32 <sup>***</sup>	-0.27 <sup>***</sup>	-0.34 <sup>***</sup>
<i>Maximum temperature</i>				
Pre-S	0.49 <sup>***</sup>	-0.11	-0.42 <sup>***</sup>	-0.41 <sup>***</sup>
Post-S	0.19 <sup>**</sup>	-0.56 <sup>***</sup>	-0.45 <sup>***</sup>	-0.53 <sup>***</sup>
ECC	0.39 <sup>***</sup>	-0.35 <sup>***</sup>	-0.48 <sup>***</sup>	-0.52 <sup>***</sup>
<i>Minimum temperature</i>				
Pre-S	-0.01	0.11	-0.20 <sup>***</sup>	0.17 <sup>**</sup>
Post-S	-0.13 <sup>*</sup>	-0.38 <sup>***</sup>	-0.03	-0.14 <sup>*</sup>
ECC	-0.07	-0.16 <sup>**</sup>	0.08	-0.01
<i>Rainfall</i>				
Pre-S	-0.26 <sup>**</sup>	0.13 <sup>***</sup>	0.60 <sup>***</sup>	0.52 <sup>***</sup>
Post-S	-0.29	0.25 <sup>***</sup>	0.59 <sup>***</sup>	0.53 <sup>***</sup>
ECC	-0.09	0.30 <sup>***</sup>	0.71 <sup>***</sup>	0.67 <sup>***</sup>
<i>Relative humidity</i>				
Pre-S	-0.26 <sup>***</sup>	0.13 <sup>*</sup>	0.39 <sup>***</sup>	0.38 <sup>***</sup>
Post-S	-0.29 <sup>***</sup>	0.25 <sup>***</sup>	0.58 <sup>***</sup>	0.57 <sup>***</sup>
ECC	-0.31 <sup>***</sup>	0.21 <sup>***</sup>	0.54 <sup>***</sup>	0.53 <sup>***</sup>
<i>Reference ET</i>				
Pre-S	0.53 <sup>***</sup>	-0.03	-0.53 <sup>***</sup>	-0.45 <sup>***</sup>
Post-S	0.56 <sup>***</sup>	-0.25 <sup>***</sup>	-0.50 <sup>***</sup>	-0.63 <sup>***</sup>
ECC	0.58 <sup>***</sup>	-0.15 <sup>**</sup>	-0.63 <sup>***</sup>	-0.57 <sup>***</sup>

<sup>a</sup> Data pooled across initial ASW scenarios.

<sup>\*</sup> Correlation at  $p < 0.05$ .

<sup>\*\*</sup> Correlation at  $p < 0.01$ .

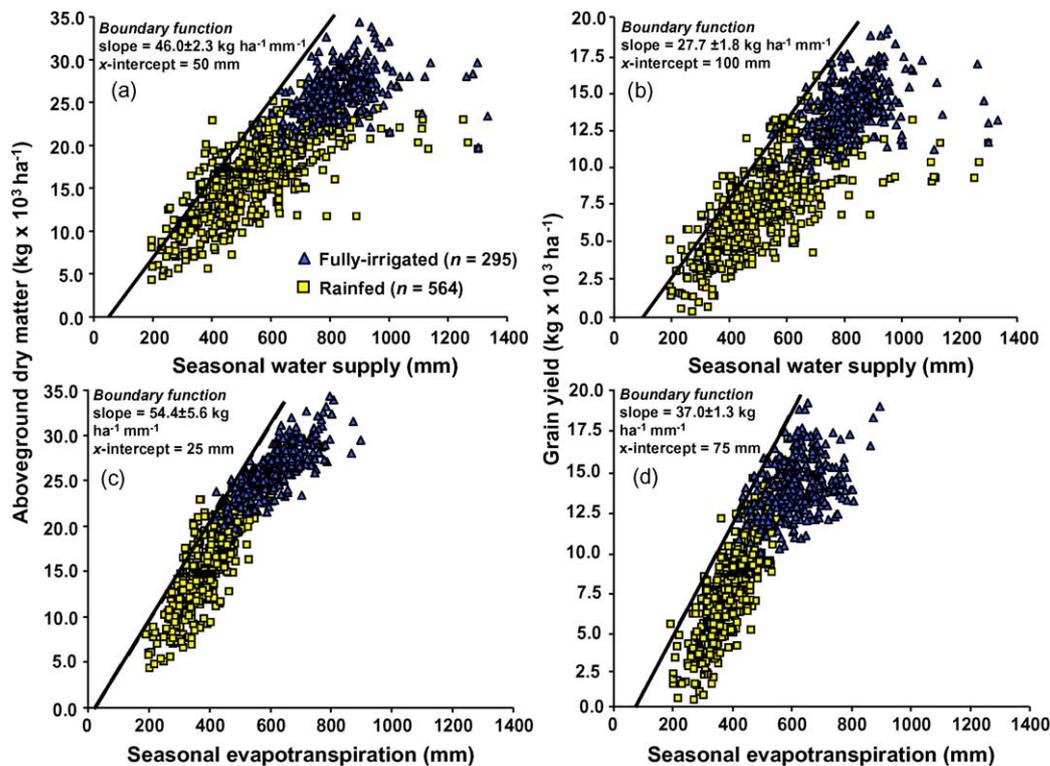
<sup>\*\*\*</sup> Correlation at  $p < 0.001$ .

The relationship between aboveground biomass or grain yield and seasonal  $ET_C$  (Fig. 6(c) and (d)) had much less scatter compared to plots against seasonal water supply (Fig. 6(a) and (b)). Fitted boundary functions for WUE based on  $ET_C$  had slopes ( $\approx TE_S$ ) of  $54.4 \pm 5.6$  and  $37.0 \pm 1.3$  kg ha<sup>-1</sup> mm<sup>-1</sup>, respectively, and  $x$ -intercepts of 25 and 85 mm ( $\approx$ seasonal soil evaporation) (Fig. 6(c) and (d)) which corresponds closely with the range of seasonal soil evaporation simulated by Hybrid-Maize for the Western Corn-Belt (range: 25–79 mm; 7–34% of the seasonal  $ET_C$ ). Across the 18 locations in our study, the mean simulated  $ET_C$  for fully irrigated crops was  $618 \pm 5$  mm, which is close to the value of 610 mm reported for irrigated maize crops grown in the Western Corn-Belt (Loomis and Connor, 1992). Although Hybrid-Maize does not account for other yield-reducing factors such as nutrient deficiencies, weeds, and pests, there was a wide range in yield of up to 6 Mg grain ha<sup>-1</sup> for both rainfed and fully irrigated crops at a given amount of  $ET_C$  (Fig. 6(c) and (d)). Hybrid-Maize simulations identified the primary causes for this variation, which include: (i) post-silking cumulative radiation and temperature under irrigated conditions, (ii) intensity of post-silking water stress under rainfed conditions, and (iii) site differences and within site annual variation in evaporative demand (determined largely by the solar radiation, vapour pressure deficit, and wind speed), and water loss from soil evaporation (data not shown).

Compared to reported values from the literature, the boundary function estimated in our current study appears to be broadly applicable to measured values of WUE from field studies conducted at a number of locations around the world (Fig. 7). Nearly all of the measured data points fell well below the attainable productivity delimited by the boundary functions for both aboveground biomass and grain yield. Despite identifying the reasons for differences in WUE across and within environments was not an objective of this paper, we speculate that gaps between the boundary function and the observed data were associated with both environmental limitations such as evaporative demand and water supply distribution, as well as other non-water-related factors such as plant population, nutrient supply, and biotic stresses. Likewise, runoff and percolation below root zone, generally not measured for  $ET_C$  calculation, contribute to the observed gap between the boundary function and actual yields, especially in locations with high rainfall.

#### 4. Discussion

Maize yields were simulated over a period of 20 years at 18 locations across the Western Corn-Belt using current best-recommended management practices for each location. Geospatial gradients in radiation, temperature, rainfall, and  $ET_O$  gradients had



**Fig. 6.** Relationships between simulated aboveground dry matter (left panels) and grain yield (right panels) and seasonal water supply (a and b), and simulated crop evapotranspiration (c and d). Rainfed crops category includes the two initial ASW scenarios. Lines are the boundary functions for water productivity (a and b), and water-use efficiency (c and d). Slopes ( $\pm$ S.E.) and x-intercepts of the boundary functions are shown. Site-years in which a frost occurred during grain filling were not included.

a large impact on maize productivity under both irrigated and rainfed conditions. Potential grain yields were closely associated with cumulative incident solar radiation and temperature during the post-silking period while rainfed grain yields were largely governed by the available water supply from initial soil moisture and rainfall.

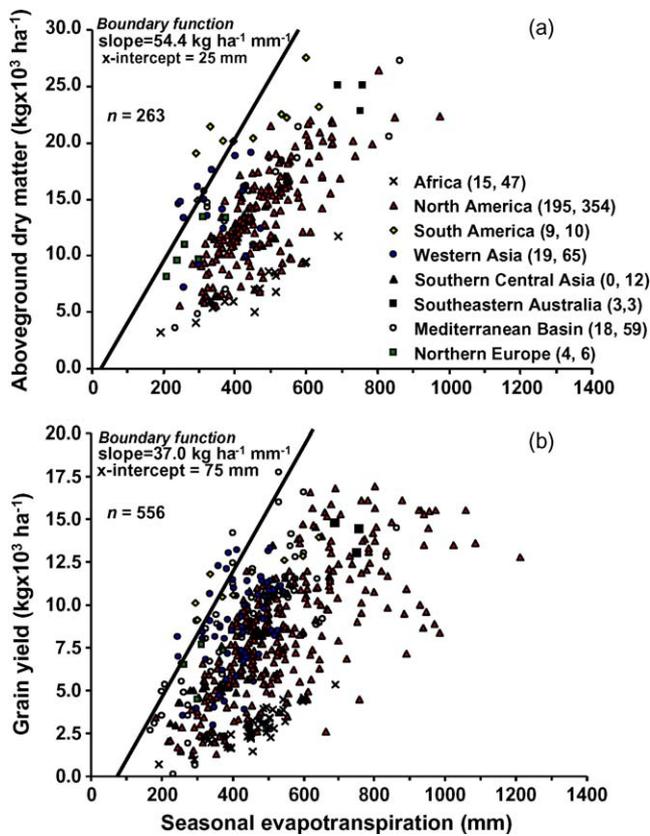
Maize maximum  $TE_s$  was estimated to be about 37 kg ha<sup>-1</sup> mm<sup>-1</sup> for grain yield, and 54 kg ha<sup>-1</sup> mm<sup>-1</sup> for total aboveground biomass. The boundary  $TE_s$  for grain yield estimated here is well above reported values for winter cereals (20–22 kg grain ha<sup>-1</sup> mm<sup>-1</sup>; Passioura, 2006; Sadras and Angus, 2006), grain legumes (12–20 kg grain ha<sup>-1</sup> mm<sup>-1</sup>; Loss et al., 1997; Zhang et al., 2000), and oilseed crops (8–13 kg grain ha<sup>-1</sup> mm<sup>-1</sup>; Specht et al., 1986; Hocking et al., 1997; Grassini et al., 2009; Dardanelli et al., 1991), which, like our maize estimates, are based on grain yields at standard commercial moisture content for each crop. Except for cases when severe water stress occurs during the sensitive anthesis-silking window (which determines maize kernel number), maize  $TE_s$  for grain yield is expected to be greater than that for other crops because maize carbon fixation occurs via the C<sub>4</sub> pathway and the energetic cost of its grain is smaller compared to protein-rich legume seed or oilseed crops (Sinclair et al., 1984; Loomis and Connor, 1992).

Analysis of yield determining factors by simulation modeling and regression analysis indicated that meteorological variables estimated separately for pre- and post-silking periods had greater explanatory power than use of estimates for the entire growing season. Whereas the greatest potential aboveground biomass yield occurs at locations and in years with a long growing-season and a late maturing hybrid, which together maximize cumulative solar radiation, warmer temperatures during the vegetative growth phase also contribute to higher potential biomass yields—presumably due to increasing photosynthetic rates and/or a more rapid leaf area expansion which

leads to an early canopy closure (Andrade et al., 1993, 1996; Westgate et al., 1997).

Based on recommended planting dates and hybrids, rainfed maize crops experience water stress during the reproductive growth period in a high proportion of years throughout the Western Corn-Belt, although the severity of stress increases along the east–west rainfall gradient. While greater stored soil water content at sowing diminishes the intensity of the water stress during the growing season, it does not eliminate it. Given the high probability of water stress, recommended rainfed plant populations decreased with the east–west rainfall gradient to avoid depletion of soil moisture during the vegetative stage due to a larger leaf area than required to achieve maximum WUE for grain yield. Field studies in Western Nebraska confirm the benefits of reducing maize plant population as the available water supply decreases (Lyon et al., 2003).

The maximum boundary functions for WP and WUE estimated in our study and regional estimates of  $ET_c$  are useful tools for diagnosing productivity constraints to maize yields in water-limited and irrigated environments. Boundary WP and WUE values provide benchmarks that can be used by agronomists and researchers to set realistic productivity goals for a specific irrigated or rainfed environment. Where measured values fall well below these thresholds, the yield gap can be closed by identifying and correcting non-water-related factors that constrain productivity, such as nutrient deficiencies, diseases, and weeds. Large differences between estimates of WP and WUE may indicate greater than average water loss from percolation, surface runoff, or a significant amount of unused water left in the soil profile at maturity. In fact, simulations showed that water losses from percolation and runoff often occur in the same year that a maize crop experiences yield-reducing water stress. Thus, management practices that reduce these losses through healthier root systems, appropriate tillage and residue management, and precise irrigation



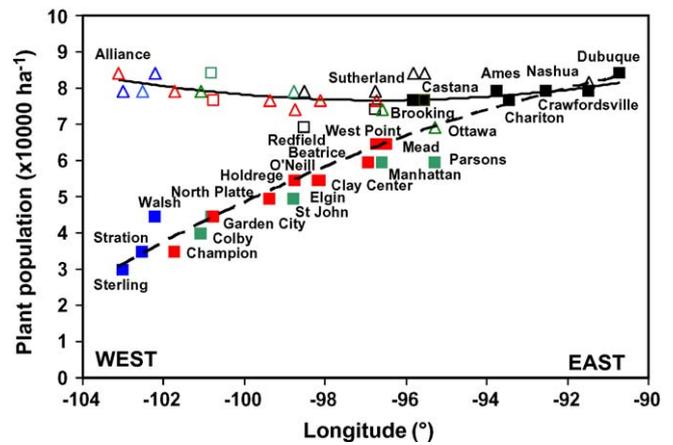
**Fig. 7.** Reported observed maize (a) aboveground dry matter and (b) grain yield/crop evapotranspiration relationships in experiments conducted in low-rainfall environments (Appendix B). For each region, the number of cases for aboveground dry matter and grain yield is indicated, in this order, between brackets. The solid lines are the boundary functions for water-use efficiency shown in Fig. 6(c) and (d); their slopes and x-intercepts are shown.

scheduling and amounts will increase the fraction of available water removed by the crop, decrease the risk or severity of water stress, and improve crop water productivity.

Overall, this study has defined the limits for maize productivity in the Western Corn-Belt. Radiation and temperature determine the ceiling for potential productivity while water supply imposes an upper limit for rainfed crops. Highest potential grain yields are expected at locations where the length of the post-silking phase is maximized, keeping temperatures over the optimum range for kernel growth and carbon net assimilation. Boundary functions derived from this study provide a useful benchmark to analyze water-limited productivity. Finally, simulated and reported data indicate that maize seasonal TE is well above to that reported for winter cereals, grain legumes and oilseed crops.

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**Fig. A1.** Actual recommended plant populations for irrigated (open triangles, solid line) and rainfed crops (solid squares, dashed line) plotted against longitude in Western U.S. Corn-Belt. Locations are named and colors indicate the state to which each location belongs (Colorado: blue; Iowa: black; Kansas: green; Nebraska: red; South Dakota: black). At some eastern locations, symbols for irrigated and rainfed crops are overlapped. Second-order polynomial functions were fitted for rainfed ( $y = -0.016x^2 - 2.65x - 101.5$ ;  $p < 0.0001$ ,  $r^2 = 0.88$ ) and fully irrigated crops ( $y = 0.013x^2 + 2.60x + 133.3$ ;  $p > 0.10$ ,  $r^2 = 0.21$ ). Both functions are shown for comparison, regardless their significance.

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### Appendix A

See Fig. A1.

### Appendix B. References that were the source of data used in Fig. 7, which plots the relationship between aboveground biomass or grain yield versus $ET_C$

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